Name	Clas	Index	
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# BROADRICK SECONDARY SCHOOL SECONDARY 4 EXPRESS / SECONDARY 5 NORMAL ACADEMIC PRELIMINARY EXAMINATION 2024

## **MATHEMATICS**

4052/01

Paper 1 Aug 2024

Candidates answer on the Question Paper

2 hours 15 minutes

#### **READ THESE INSTRUCTIONS FIRST**

Write your name, class and index number on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

Answer all questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

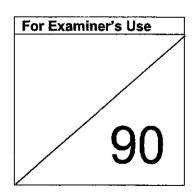
The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142, unless the question requires the answer in terms of  $\pi$ .

The number of marks is given in brackets [ ] at the end of each question or part question. The total of the marks for this paper is 90.

For Examiner's U	se	
Error In	Question Number	Marks Deducted
Rounding-off		
Reasoning		
Presentation		



This document consists of 21 printed pages.

Setter(s):

## Mathematical Formulae

Compound interest

Total amount = 
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved Surface area of a cone =  $\pi r l$ 

Surface area of a sphere =  $4\pi r^2$ 

Volume of a cone = 
$$\frac{1}{3}\pi r^2 h$$
  
Volume of a sphere =  $\frac{4}{3}\pi r^3$ 

Area of triangle 
$$ABC = \frac{1}{2}ab \sin C$$

Arc length =  $r\theta$ , where  $\theta$  is in radians

Sector area = 
$$\frac{1}{2}r^2\theta$$
, where  $\theta$  is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

**Statistics** 

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation = 
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

# Errata Q13b -- For P>10 instead of P>/= 0

Answer	zer all	l the	questions	١.
Answer	zer all	l the	questions	

	Answei an the questions.	
1	Evaluate $\frac{(-3.85)^2 - \sqrt{10 - 0.9 \times (-6)}}{3.11 - 4^3}$ , giving your answer to 4 significant figures.	
	Answer	[1]
	The frequency table shows the reaction time, $t$ seconds, for a chemical to change the colour of the litmus paper in 100 laboratory sessions. $time(t sec)  0 < t \le 1  1 < t \le 2  2 < t \le 3  3 < t \le 4  4 < t \le 5$ Frequency 8 28 44 18 2  Calculate an estimate for the  (a) mean reaction time,	
	Answers  (b) standard deviation of the reaction times.	[1]
	<i>Answer</i> s	[1]
3	Given that $\frac{5^x}{2^{2x} \times 5^{3-x}} = 2^m 5^n$ , express $m$ and $n$ in terms of $x$ .	
	Answer m =	
	n =	[2]

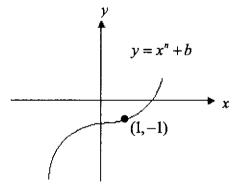
4	The Both	highest common factor of two numbers is 18. lowest common multiple of the two numbers is 324. numbers are greater than 20. the two numbers.
		Answer and [2]
5	A m	ap has a scale of 1:50 000.
	(a)	The distance between two towns on the map is 7.5 cm. Calculate the actual distance between the two towns in kilometres.
	<b>a</b> .\	Answer
	(b)	A lake covers an actual area of 2.25 square kilometres. Find the area of the lake on the map in square centimetres.

Answer		cm <sup>2</sup>	[2]
2111077761	*************	OIII	

A wooden block has a mass of 115 grams, correct to the nearest gram. The volume of the block is 6 cm<sup>3</sup>, correct to the nearest cm<sup>3</sup>. Find the largest possible density of the block in g/cm<sup>3</sup>.

$$Density = \frac{Mass}{Volume}$$

7 In the following graph, write down a possible value of n and the corresponding value of b for the equation.



	In triangle $ABC$ , $AB = 14.6$ cm, $BC$		
	Find (a) obtuse angle ACB,	A 14.6	7.6
	(b) area of triangle ABC.	Answer°	[2]
		Answercm <sup>2</sup>	[2]
9	is   1 = 0.0086.	oan. e dollars (\$) into Yen (¥). \$100 = ¥11600 and the exchange rate in Japan ore if she changes the money in Singapore.	
9	She wants to change 850 Singapore is 3 is \(\frac{1}{2}1 = \\$0.0086.\) She claims that she will receive modulatify if her claim is true.	e dollars (\$) into Yen (¥). \$100 = \$11600 and the exchange rate in Japan	

	ee consecutive years.		ass B over	
	Class A			
		70		
		65	CI D	
			Class B	
(a)	What feature of the graph misleads reader 2022 had increased to 6 times that in 2024		scores of Class	<i>A</i> in
				. [1]
(b)	Hailey claims that the scores of Class A a improvement from 2022 to 2024.  Do you agree?  Explain your answer.	nd Class B shows t	he same	. [1]
(b)	improvement from 2022 to 2024. Do you agree?	nd Class B shows t	he same	. [1]
<b>(b)</b>	improvement from 2022 to 2024. Do you agree?	nd Class B shows t	he same	. [1]
(b)	improvement from 2022 to 2024. Do you agree?	nd Class B shows t	he same	. [1]
(b)	improvement from 2022 to 2024. Do you agree?	nd Class B shows t	he same	. [1]

11	The number $2^p \times 5^q \times \frac{5}{2}$	is a perfect cube where $p$ and $q$ are greater than 1.
	Find the smallest possib	le integer values of $p$ and of $q$ .

Answer	<i>p</i> =	
	<i>q</i> =	[2]

12 (a) Simplify  $(16y^3)^{\frac{3}{2}}$ .

Answer .....[1]

(b)  $5^k = 125\sqrt[3]{5\sqrt{5}}$ Use laws of indices to find the value of k. Show your working.

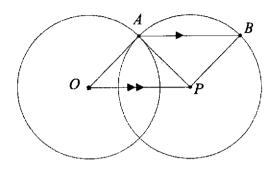
13	A = B = B	en that $\xi = \{\text{integers } x: p \le x < 20 \}$ $\{\text{factors of 24}\}$ $\{\text{prime numbers}\}$ $\{\text{perfect squares}\}$	Answer	k =	[3]
	(a)	List the elements of $A$ if $p = 2$ .			
			Answer		[1]
	(b)	For $p \ge 0$ , list the elements of $(B \cup \{a\})$	C)' such 1	that $n(B \cup C)' = 4$ .	
	(c)	Find the smallest $p$ such that $A \cap C$			[1]
<del></del>			Answer	<i>p</i> =	[1]

14 A company divided a bonus among its employees A, B, and C in the ratio 2:3:
7.
C's bonus was X% more than the combined bonus of A and B.
Find X.

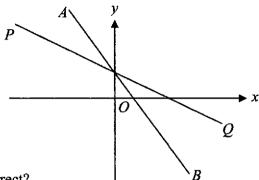
Answer  $X = \dots$  [2]

15 In the diagram, two circles with centres O and P respectively intersects at A. The two circles have the same radius and AB // OP. Show that AB = OP.

Answer



16 (a) Leanne says that the equation of the line AB is 2y = -4x + 1 and the equation of the line PQ is 4y = -9x + 2.

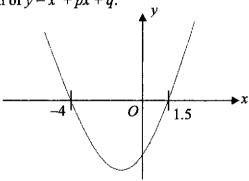


Is she correct?

Explain your answer.

***************************************	
	[2]

**(b)** The diagram shows the graph of  $y = x^2 + px + q$ .



(i) Write down equation of the graph in the form  $y = x^2 + px + q$ .

Answer		[2]
--------	--	-----

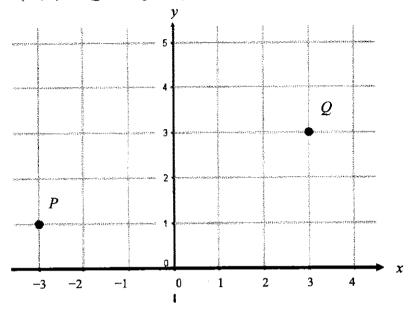
(ii) Find the coordinates of the minimum point.

17					
	Write as a single	fraction	in its	simplest form	ı

					F23
			Answer		[2]
18	(a)	Factorise completely.			
		(i) $24a^2b+12ab^2-ab$			
			Answer		[1]
		(ii) $mn-18-9m+2n$	,		
		(II) mil 10 m 2n			
			Answer	***************************************	[2]
	(b)	Expand and simplify $(-2x+3q)(x-4)$	(2q).		
			Answer		[2]

			13		
19	Raye	den invested \$20 000 at a rate of 0.3 Find the value of his investment a			
	(b)	Rayden then withdrew $\frac{1}{5}$ of the a Find the new rate of compound in investment reaches the same value.	ccumulated a	nth so that his remaining	[2]
		$2x^2 - 5xy - 12y^2$	Answer	%	[2]
20	Sim	plify $\frac{2x^2 - 5xy - 12y^2}{x^2 - 16y^2}$ .			

21 P is the point (-3, 1) and Q is the point (3, 3).



(a) Find the length of the PQ.

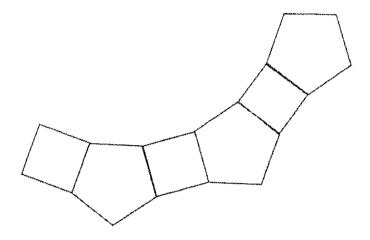
Answer	units	[2]
answer	units	L∠J

(b) The point R is such that PQR forms an isosceles triangle. The angle bisector of angle PQR has an equation of y = x. Find the coordinates of R.

Answer (...... [1]

22 Regular pentagons and squares of the same sides are placed together in a pattern as shown in the diagram.

Caleb claims that if he continues the pattern, a closed loop will form. Explain whether his claim is true, showing your working clearly.



Answer

,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	
·····	
	Г3
>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>	LJ.

23	A cylinder $X$ has radius, $r$ cm and height $h$ cm.
	A hemisphere $S$ is such that its radius is half of the radius of cylinder $X$ .

(a) The volume of the cylinder is 4 times that of the hemisphere. Express h in terms of r.

Answer	h = .	 [3]	

(b) Another cylinder Y is geometrically similar to cylinder X. The ratio of the curved surface area of X: Y = 9: 4. Find the height of cylinder Y in terms of r.

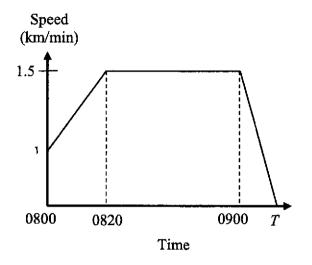
Answer ......[2]

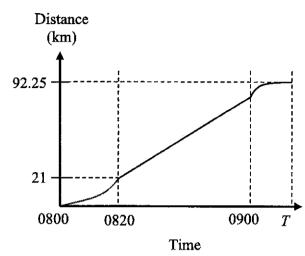
24	The	The sum of the first $n$ terms of a linear sequence is $ ext{.}$					
	(a)	Show that the sum of the first $n$ terms in the sequence is always even.					
		[2]					
	(b)	By finding the first three terms in the sequence or otherwise, find, in terms of $n$ , an expression for the $n$ th term of the sequence.					
		4					
		Answer[2]					

25	In bookstore A, a fiction book costs \$8, a non-fiction book costs \$10 and a science book costs \$11.50.						1	
	In bookstore B, a fiction book costs \$1.10 less, a non-fiction book costs \$2.80 less and a science book costs \$1.50 more than that in bookstore A.							ıa
	a scit	the book costs \$1.50 more than that in	DOORBIO		Α	В		
							F	
							NF	
	The i	nformation can be represented by the ma	atrix				S	
		,						
	(a)	Kevin bought 4 fiction books, 3 non-fice Molly bought 2 fiction book and x scient Represent their purchases, in terms of x	nce book	ζS.		ce books.		
		A	nswer	<b>P</b> =				[1]
	(b)	Evaluate the matrix $\mathbf{R} = \mathbf{PQ}$ .						
			Inswer	<b>R</b> =				[2]
	(c)	Explain what the elements in the first of	column (	of mati	rix <b>R</b> rep	oresent.		
			••••••	••••••				
					•••••		•••••	[1]
	(d)	Molly can save \$5.30 by purchasing in Using your answer in (b), find the valu		ore A.				
		A	Answer	<i>x</i> =				[1]

26 The diagrams show the speed-time graph and the corresponding distance-time graph of a car.

The car travelled from a point P to Q and in the journey, its greatest speed attained was 1.5 km/min.





(a) Convert 1.5 km/min to m/s.

Answer .....m/s [1]

(b) Show that v, the initial speed, was 0.6 km/min.

[2]

(c) Find the speed of the car, in m/s, at 0812.

Answer ......m/s [2]

(d) The total distance travelled by the car is 92.25 km. Find the time, T, when it comes to a complete stop.

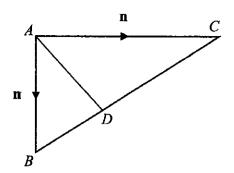
Answer ......[2]

27 ABC is a triangle.

D is the point on BC such that 3BD = 2DC.

and

(a) Find  $\stackrel{\sim_{\text{MODUL}}}{AD}$  in terms of **m** and **n**.



Answer	***************************************	[2]
--------	---	-----

- (b) R is on AD produced such that AR = kAD and AC is parallel to BR.
  - (i) Show that  $k = \frac{5}{3}$ .

    Answer

[3]

(ii)  $\frac{\text{area of triangle } ABD}{\text{Find the ratio}}$  area of triangle RBD.

Answer ......[1]

End of Paper

Paper 1 Ar	iswer Key
1	-0.17898 = -0.1790
2a	228
	Mean = $\overline{100}$ = 2.28 s
b	0.901 s (3sf)
3	m = -2x
	n=2x-3
4	$X = 2^2 \times 3^2 = 36$
	$Y = 2 \times 3^4 = 162$
5a	3.75 km
b	9 cm <sup>2</sup>
6	21 g/ cm <sup>3</sup>
7	n=3 or 5 (any odd integer more than 1)
	b = -2
8a	98.3° (1dp)
b	42.9 cm <sup>2</sup> (3sf)
9	Her claim is not true. She will receive (237.21 Yen) more
	if she changes in Japan.
10a	The vertical axis did not start from 0.
	(Optional: The scores in 2022 looked like it had increased
	to 6 times but the increase was from 55 to 80 (which is
	slightly less than double.)
b	I disagree.
	Although the increase in the height of the bar looks the
	same from 2022 to 2024 for both classes, the scale of the two graphs are different. It exaggerates the increase in
	two graphs are different. It exaggerates the increase in test scores of Class B.
11	p = 4
11	*
	q=2
12a	$64y^{\frac{9}{2}}$
b	$k=3\frac{1}{2}$
	$k=3\frac{7}{2}$
13a	A={2,3,4,6,8,12}
b	$(B \cup C)' = \{12,14,15,18\}$
c	smallest p = 5
14	40%
15	$\Delta OPA \equiv \Delta BAP \text{ (AAS)}$
	Hence $AB = OP$
16a	The gradient of $PQ$ should be steeper than that of $AB$ .
	Hence she is not correct.
bi	$y = x^2 + 2.5x - 6$
bii	Min point (-1.25, -7.5625)
17	$=\frac{4x^2-10x+4}{(3x-1)(2x+1)}$
	(3x-1)(2x+1)

18ai	=ab(24a+12b-1)
aii	(m+2)(n-9)
ь	$=-2x^2+7xq-6q^2$
19a	= \$21490.79 (2dp)
Ъ	r = 0.622%
20	
	$=\frac{2x+3y}{x+4y}$
21a	= 6.32 units (3sf)
Ъ	R  is  (1, -3)
22	$n = \frac{360}{18} = 20$
	Since n is a positive integer, it is possible to form a regular polygon, hence a closed loop.
23a	$h = \frac{1}{3}r$
b	$H = \frac{2}{9}r$ $5n^2 - n = n(5n - 1)$
24a	$5n^2 - n = n(5n-1)$
b	10n-6
25a	$ \begin{array}{c cccc} 10n-6 & & & \\ P = \begin{pmatrix} 4 & 3 & 2 \\ 2 & 0 & x \end{pmatrix} & & \\ \hline \begin{pmatrix} 85 & -9.8 \\ 16+11.5x & 2.2+1.5x \end{pmatrix} \end{array} $
b	$= \begin{pmatrix} 85 & -9.8 \\ 16+11.5x & -2.2+1.5x \end{pmatrix}$
С	It represents the amount of money Kevin and Molly spent respectively at Bookstore A.
d	x = 5
26a	25 m/s
b	Area = dist travelled
c	19m/s
d	T is 0915
27a	$=\frac{3}{5}\mathbf{m}+\frac{2}{5}\mathbf{n}$
bii	
	$\frac{3}{2}$
	2

Name	Γ	Clas			Index	
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# BROADRICK SECONDARY SCHOOL SECONDARY 4 EXPRESS / SECONDARY 5 NORMAL ACADEMIC PRELIMINARY EXAMINATION 2024

# **MATHEMATICS**

4052/02

Paper 2

Aug 2024

Candidates answer on the Question Paper.

2 hours 15 minutes

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Write in dark blue or black pen.

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The total of the marks for this paper is 90.

Error In	Question Number	Marks Deducted
Rounding-off		
Reasoning		
Presentation		

For	For
Candidate'	Examiner's
s Use	Use Use
Question	Marks
	Obtained
Number 1	/5
·	
2	/10
3	/10
4	/9
5	/9
6	/10
7	/10
8	/10
9	17
10	/10
Total Marks	/90

This document consists of 22 printed pages.

Setter(s): Ms Yeo Li Shan

### Mathematical Formulae

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Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Statistics

$$Mean = \frac{\sum fx}{\sum f}$$

Standard deviation = 
$$\sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

# Answer all the questions.

1

	ompany produces phones.  023, the company produced 3.6 million smartphones.	
(a)	Due to increased demand, the company produced 4.2 million smartphones in 2024.  Express this production figure in standard form.	
	Answer	[1]
(b)	Calculate the percentage increase in smartphone production from 2023 to 2024.	
	Anguar 9/	ro]
(c)	Answer%  In 2023, 4% of the total phones produced were not smartphones.  Calculate the total number of phones produced in 2023.  Express your answer in standard form.	[2]
	Answer	[2]

BP~	1	6	6
-----	---	---	---

4

2	(a)	Solve
	• •	JULVE

Answer 
$$x = \dots$$
 [2]

(b) Solve the inequality  $1-3p \ge 5$ .

 $(c) \qquad 3A = \frac{Ap+h}{1-h}$ 

Rearrange the formula to make A the subject.

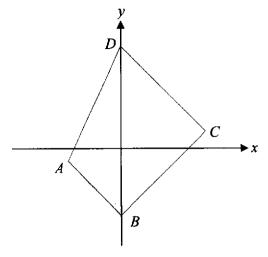
Answer 
$$A = \dots$$
 [3]

(d)

Solve the equation . Give your answers correct to two decimal places.

Answer x = or [4]

- 3 A is the point and D is the point B is a point on the y-axis.
  - (a) The line AB is parallel to 3y + 5x 6 = 0. Find the equation of the line AB.



Answer	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	[3
TIMITO	, , , , , . ,	-

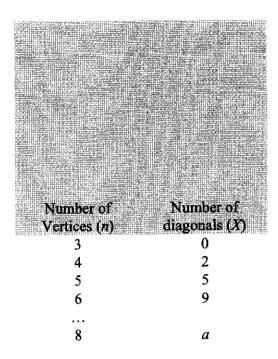
(b) Find the coordinates of C such that it is equidistant from B and D and it lies on the line y = 7.5 - x.

Answer (.....) [2]

(c)	Find the area of the quadrilateral AB	PCD.		
(d)	Find the size of angle ABC.	Answer	units²	[2]
	Ü			
		Answer	°	[3]

4 The table below shows the number of vertices (n) and number of diagonals (X) in

a polygon.



(a) Write down the value of a.

- (b) The number of diagonals is related to the number of vertices by the equation  $X = pn^2 + qn$  where p and q are constants.
  - (i) Using appropriate substitution, show that 16p + 4q = 2 and 25p + 5q = 5.

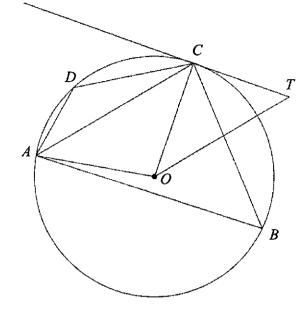
    Answer

(ii) Solve these simultaneous equations to find the values of p and of q.

	Answer	n =	
	2111311401	P	
		q =	[2]
		<i>q</i> =	[3]
			[3]
(iii) Explain whether it is possible t	o have a n		[3]
(iii) Explain whether it is possible to 495 diagonals.	to have a n		[3]
495 diagonals.	to have a n		[3]
(iii) Explain whether it is possible to 495 diagonals.  Show your working clearly.	o have a n		[3]
495 diagonals.	o have a n		[3]
495 diagonals.	to have a n		[3]
495 diagonals.	o have a n		[3]
495 diagonals.	o have a n		[3]
495 diagonals.	o have a n		[3]
495 diagonals.	o have a n		[3]
495 diagonals.	o have a n		[3]
495 diagonals.	o have a n		[3]
495 diagonals.	to have a n		[3]
495 diagonals.	o have a n		[3]
495 diagonals.	to have a n		[3]
495 diagonals.	to have a n		[3]

In the diagram, A, B, C and D are points on the circle with centre O. CT is tangent to the circle and AC is parallel to OT.

Angle  $AOC = 100^{\circ}$ .



(a) Giving reason(s) for your workings, find

(i) angle ABC,

Answer	Angle	ABC	=	[1]
		0		

(ii) angle ADC,

Answer Angle 
$$ADC = [1]$$

(iii) angle OTC.

		Answe	r Angle	OTC	=	[3]
<b>(b)</b>	Explain whether a circle c	an be drawn passii	ng through tl		, $C$ and	D.
*****				***************		
				************		
			••••••	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		
•••••			•••••	***************		[1]
(c)	Given $CT = 4.8$ cm, find	the area of the min	or segment	ADC.		

Answer ...... cm<sup>2</sup> [3]

6	(a)	Complete the table of values for	$y = \frac{1}{x - 1} + x - 1$	l
U	( <i>a</i> )	Complete the table of values for	$y = \frac{1}{x-1} + x$	

x	-2	-1	0	0.5	0.75	1.25	1.5	2	3	3.5	4
y		-2.5	-2	-2.5	-4.25	4.25	2.5	2	2.5	2.9	3.33

(b) On the grid opposite, draw the graph of  $y = \frac{1}{x-1} + x - 1$  for  $y = \frac{-2 \le x \le 4}{-2}$  [3]

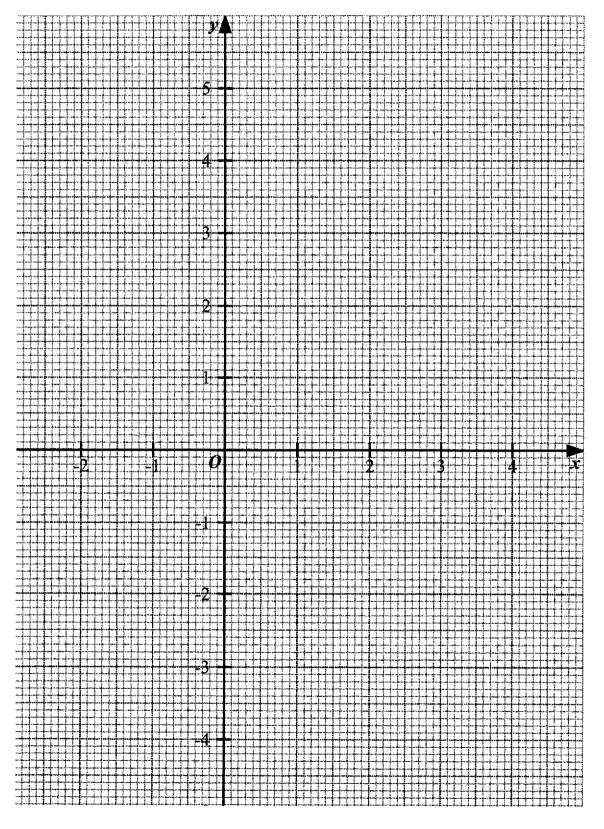
(c) The point P has the coordinates (-1, 2). A tangent to the curve can be drawn so that the tangent passes through P and its gradient < 0.

(i) Draw this tangent on the same grid. [1]

(ii) Find the equation of this tangent.

Answer .....[2]

(d) By drawing an appropriate line, use your graph to solve the equation  $\frac{1}{x-1} - \frac{1}{4}x = 0$  in the range

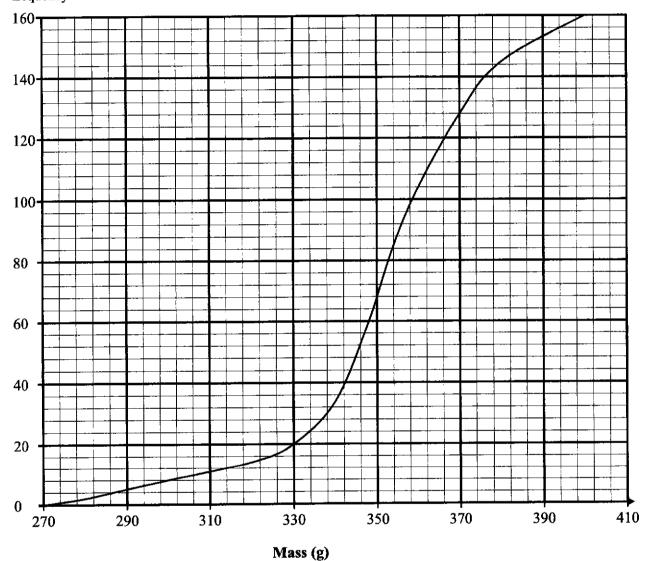


Broadrick Secondary School, Preliminary Examination 2024, Sec Four Express/ Five Normal (Academic), Mathematics Paper 2

[Turn Over]

7 The cumulative frequency curve shows the distribution of the masses of 160 apples in tree A.





- (a) Use the curve to estimate
  - (i) the median mass,

Answer		[1]
	g	

(ii) the interquartile range of the masses.

	(b)	Answer 20% of the heaviest apples belong to the top Find the minimum mass an apple needs to be	g grade.	[2]
	(c)	Two apples are chosen at random.	g	[2]
		Find the probability that one apple weighs apple weighs more than 360 g.  Give your answer to 3 significant figures.	less than 320 g and the other	er ·
20 ⊨		Answer masses of 160 apples from tree B were record box-and-whisker plot shows the distribution of	led.	. [2]
18 16 14				
10 F 260	(d)	280 300 320 340 Explain if the following statement is true. "In tree B, there are more apples weighing those weighing more than 360 g."	360 380 less than 320 g as compared to	400 420
	******			[1]
	(e)	Justine claims that it is better to get the apple Do you agree? Explain your answer using appropriate figure		
				•

10 cm.	open lid such that I and		neasuring 15 cm by 8 cm by	[
A rod is placed Assume that the	inside the box such that e rod has negligible widt	it touches th h.	e box only at $A$ and $J$ .	
(a) Find the	E $A = 15$ ength of $BE$ .	C	G 10 F 8	
		Answer		

	Answer	[2]
	cm	
(c)	Show that the length of the rod, $AJ$ , is 22.97 cm, correct to 4 significant figures.	
	Answer	

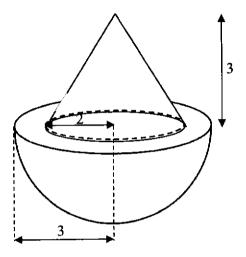
[4]

(d) Find angle JAG.

4	0	[2]
Answer		[4.]

An upright container is in the shape of a cone, mounted on a hemisphere. The centre of the base of the cone and the hemisphere coincides. The cone has a radius of 2 m and height of 3 m.

The hemisphere has a radius of 3 m.



(a) Find the capacity of the container.

' [2	[;
3	³ [2

(b)	There is a tap on the vertex of the cone.
(0)	The container is filled with water such that the hemisphere and 90% of the
	cone are filled.
	Find the area which the water is in contact with the container.

Answer ..... m<sup>2</sup> [5]

- 1 Tay is part of a student committee organizing a charity race event in 2025.
- 0 He wants to estimate the cost per participant to cover all expenses.

He did some more research and found the following costs.

Costs (excluding 9% GST)			
Item	Description	Unit cost	
Printing of T-shirts	One sided print Bundle of 100 pcs	\$800	
	Double sided print Bundle of 100 pcs Bundle of 500 pcs	\$1500 \$7000	
Goodie bags (Pack of 5)	One pack of 5 bags Bulk price (100+ packs) Bulk price (500+ packs)	\$20 \$18 \$15	
Booking of venue	At least 6 months in advance 3 to 5 months in advance	\$1200 \$1500	
Refreshments	Large set Regular set Small set	\$3 \$2.80 \$2.50	
Participant medals	Pack of 10 Pack of 50	\$45 \$210	

The T-shirts are printed overseas and shipped by a local courier.

Tay estimated the weight of each shirt to be 140 grams and he needs to select one of the local couriers.

The shipping rate depends on the weight of the product and courier.

Local Courier	First kg	Next 0.5 kg	Weight Limit of
	<del>-</del>		each parcel*
Simply Post	\$4.80	\$1.85	80 kg
Singapore Post	\$6.00	\$1.80	50 kg
DPEX	\$5.50	\$1.60	30 kg

<sup>\*</sup>Products need to be shipped in separate parcels if weight exceeds the limit. 9% GST is applicable for import goods as well as shipping fees.

(a)	How many percent more will Tay need to pay if he booked the venue 3
	months in advance instead of 6 months in advance?

Answer ...... % [1]

(b) For a 50 kg purchase, calculate the amount of shipping fees charged by Singapore Post.

Answer \$ [2]

The event is scheduled to be in October.

Tay estimated the number of participants to be 1000 and he plans to confirm the venue by February.

He also wants to print double sided for the participant's T-shirt, and issue a goodie bag, refreshment and medal to each participant.

He needs to decide how much registration fee he should charge each participant. He must be able donate at least 40% of the proceeds to the charity and still cover all the costs.

(c) Suggest a sensible amount for the registration fee of a participant. State your assumptions and decisions if any. Show your calculations clearly.

Answer	\$	[7]

End of Paper

## Broadrick Secondary School

# 4E5N Preliminary Examination 2024

## Paper 1 Marking Scheme

1	-0.17898 = -0.1790 (4sf)	B1
2a	228	B1
	Mean = 100 = 2.28 s	
b	$\sqrt{\frac{601}{100} - (2.28)^2} = 0.901 \text{ s (3sf)}$	B1
3	$\frac{5^x}{2^{2x} \times 5^{3-x}} = 2^m 5^n$	
	$2^{-2x}5^{x-(3-x)}=2^m5^n$	
	m = -2x	B1
	n=2x-3	B1
4	HCF = $18 = 2 \times 3^2$	
	LCM = $324 = 2^2 \times 3^4$	
	V 2 <sup>2</sup> 2 <sup>2</sup> 00	
	$X = 2^2 \times 3^2 = 36$	B1
	$Y = 2 \times 3^4 = 162$	B1
5a	1:50 000	
	1cm: 0.5 km	
	Actual dist = $7.5 \times 0.5 = 3.75$ km	B1
b	1cm: 0.5 km	
	1 cm <sup>2</sup> : 0.25 km <sup>2</sup>	M1
	Area on map = $2.25 \div 0.25 = 9 \text{ cm}^2$	A1
6	Largest density = largest mass/smallest vol	
	$=\frac{115.49}{5.5} = \frac{115.5}{5.5}$	
		M1
	= 21 g/ cm <sup>3</sup>	A1
7	n=3 or 5 (any odd integer more than 1)	B1
	$-1 = (1)^3 + b$	B1
	b = -2	
8a	$\frac{\sin \angle ACB}{\sin 31} = \frac{\sin 31}{\sin 31}$	M1
	14.6 7.6	
	$\angle ACB = 81.6562$	A1
L	Obtuse $\angle ACB = 180 - 81.6562 = 98.3438 = 98.3^{\circ}$ (1dp)	1,,,

b	Angle $ABC = \angle ACB = 180 - 31 - 98.3438 = 50.6562$ Area = $\frac{1}{2}(14.6)(7.6)\sin(50.6562)$	M1 (formula to find area with their angle)
	=42.9 cm² (3sf)	
9	In Singapore: $Amount of Yen = \frac{850}{100} \times 11600 = 98600$	M1
	In Japan Amount of Yen = $\frac{850}{0.0086} \times 1 = 98837.21$	M1
	98837.21 > 98600  Her claim is not true. She will receive (237.21 Yen) more if she changes in Japan.	A1
10a	The vertical axis did not start from 0. (Optional: The scores in 2022 looked like it had increased to 6 times but the increase was from 55 to 80 (which is slightly less than double.)	B1
b	I disagree. Although the increase in the height of the bar looks the same from 2022 to 2024 for both classes, the scale of the two graphs are different. It exaggerates the increase in test scores of Class B.	B1
11	$2^{p} \times 5^{q} \times \frac{5}{2}$ perfect cube (powers are multiples of 3) p = 4 a = 2	B1 B1
12a	$(16y^3)^{\frac{3}{2}} = 64y^{\frac{9}{2}}$ $5^k = 125\sqrt[3]{5\sqrt{5}}$	B1
b	$5^{k} = 5^{3} \left( 5(5)^{\frac{1}{2}} \right)^{\frac{1}{3}}$	M1 (change either to power of 3)
	$5^k = 5^3 \left(5^{\frac{3}{2}}\right)^3$	M1 (combine to
	$5^k = 5^3 \left(5^{\frac{1}{2}}\right)$ $k = 3\frac{1}{2}$	5 <sup>2</sup> or to a single power of 3)
		A1

13a	A={2,3,4,6,8,12}	B1
b	Since $p \le x < 20$ , B={,11, 13, 17, 19} C={,9, 16} $(B \cup C) = \{,9,11,13,16,17,19\}$	
	$(B \cup C)' = \{12,14,15,18\}$	B1
С	A={2,3,4,6,8,12} C={4,9,16}	
	If $A \cap C = \emptyset$ , smallest p = 5	B1
14	If $A \cap C = \emptyset$ , smallest p = 5 $X = \frac{7-5}{5} \times 100\%$	M1
	= 40%	A1
15	In triangle OAP and BPA,	
	* $\angle OPA = \angle BAP$ (alt angle, AB // OP)	B2 (any 2 of the 3 stmts)
	Since $OA = AP = PB$ (same radius). * $\angle AOP = \angle PBA$ (base angles of isos triangle) * $AP = PA$ (common side)	
	Therefore $\triangle OPA \equiv \triangle BAP$ (AAS)	A1 (conclude AAS and equal sides)
	Hence AB = OP	
16a	2y = -4x + 1	M1 (rearrange
	AB: $y = -2x + \frac{1}{2}$	to find gradient of either line)
	4y = -9x + 2	
	$PQ: \ y = -\frac{9}{4}x + \frac{1}{2}$	
	The gradient of PQ should be steeper than that of AB. Hence she is not correct.	A1 (compare both gradient and conclude)

1. !	(-, 1.4)(-, 1.5)	M1
bi	y = (x+4)(x-1.5)	A1
	$y = x^2 + 2.5x - 6$	B1, B1
bii	Min point (-1.25, -7.5625)	DI, D1
17	$\frac{2x}{2} - \frac{4}{2}$	ļ
	3x-1 $2x+1$	
	$=\frac{2x(2x+1)-4(3x-1)}{(3x-1)(2x+1)}$	M1
	$=\frac{4x^2+2x-12x+4}{(3x-1)(2x+1)}$	
	(3x-1)(2x+1)	
	$4x^2 - 10x + 4$	
	$=\frac{4x^2-10x+4}{(3x-1)(2x+1)}$	A1
18ai	$24a^2b + 12ab^2 - ab$	
	=ab(24a+12b-1)	B1
aii	mn-18-9m+2n	
	= mn - 9m + 2n - 18	M1 (grouping)
	= m(n-9) + 2(n-9)	M1 (grouping)
	=(m+2)(n-9)	A1
b	(-2x+3q)(x-2q)	
	$= -2x^2 + 4xq + 3qx - 6q^2$	M1
	$=-2x^2+7xq-6q^2$	A1
19a	$A = P(1 + \frac{r}{100})^n$	
	$=20000\left(1+\frac{0.3}{100}\right)^{24}$	M1
	=21490.79038	
	= \$21490.79 (2dp)	A1
b	$A = \frac{4A}{5} \left(1 + \frac{r}{100}\right)^{36}$	M1
	$\frac{5}{4} = (1 + \frac{r}{100})^{36}$ $\sqrt[36]{\frac{5}{4}} = 1 + \frac{r}{100}$ $\sqrt[36]{\frac{5}{4}} - 1 = \frac{r}{100}$	
	$\sqrt[36]{\frac{5}{4}} = 1 + \frac{r}{100}$	
	\( \sqrt{5} \)	
	$\frac{36}{3} \frac{3}{4} - 1 = \frac{7}{100}$	
	177 100	A1
	r = 0.622%	
20		
L		

	T 2	
	$\frac{2x^2 - 5xy - 12y^2}{x^2 - 16y^2}$	M1, M1
	$= \frac{(x-4y)(2x+3y)}{(x+4y)(x-4y)}$	A1
	$=\frac{2x+3y}{x+4y}$	
	x+4y	
21a	$PQ = \sqrt{(-3-3)^2 + (1-3)^2}$	M1
:	= 6.32 units (3sf)	A1
b	R is (1, -3)	B1
	By sketching and counting,	
	From Q to P: horizontally -6 and vertically -2	
	Since y=x is reflection line,	
	From Q to R: horizontally -2 and vertically -6	
22	$= \frac{(5-2)\times180}{5} = 108^{\circ}$	M1
	int angle of pentagon 5	
	Int angle of square = 90°	
	Interior angle of regular polygon =	M1 (int or ext of
	360-90-108=162°	polygon)
	Exterior angle = $180 - 162 = 18^{\circ}$	
	$n = \frac{360}{18} = 20$	
	$\frac{n-18}{18} = 20$	
	Since n is a positive integer, it is possible to form a	A1
23a	regular polygon, hence a closed loop.	NA4 NA4
230	$\pi r^2 h = 4 \left( \frac{2}{3} \pi \left( \frac{1}{2} r \right)^3 \right)$	M1, M1
	` /	
	$\pi r^2 h = \frac{8}{3} \pi \left( \frac{1}{8} r^3 \right)$	
	· '	
	$h = \frac{8}{3} \left( \frac{1}{8} r \right)$ $h = \frac{1}{3} r$	
	. 1	
	$n = \frac{1}{3}r$	A1
b		M1
	<u> </u>	J

	$\frac{4}{9} = \left(\frac{H}{h}\right)^2$	A1
	$\frac{H}{h} = \frac{2}{3}$	
ŗ	$H = \frac{2}{3}h = \frac{2}{3}\left(\frac{1}{3}r\right)$	
:	$H = \frac{2}{9}r$	
24a	$5n^2 - n = n(5n - 1)$ When n is odd,	M1
	5n is odd and 5n-1 is even	
	Since product of odd and even number is always	
	even, $n(5n-1)$ is even.	
	When n is even,	
	5n is even and 5n-1 is odd.	
	Since product of odd and even number is always	
	even, $n(5n-1)$ is even.	A1
	Hence the sum of the first <i>n</i> terms in the sequence is always even.	
b	1st term: $5(1)^2 - 1 = 4$	
	<b>2</b> <sup>nd</sup> term: $5(2)^2 - 2 - 4 = 14$	M1
	$3^{rd}$ term: $5(3)^2 - 3 - 14 - 4 = 24$	
	Therefore $= 10n - 6$	A1
25a	$P = \begin{pmatrix} 4 & 3 & 2 \\ 2 & 0 & x \end{pmatrix}$	B1
b	( 0 11 )	
	$\mathbf{R} = \mathbf{PQ} = \begin{pmatrix} 4 & 3 & 2 \\ 2 & 0 & x \end{pmatrix} \begin{pmatrix} 8 & -1.1 \\ 10 & -2.8 \\ 11.5 & 1.5 \end{pmatrix}$	
	$= \begin{pmatrix} 85 & -9.8 \\ 16+11.5x & -2.2+1.5x \end{pmatrix}$	B2 (B1 for any 2 correct)
		<u>'</u>
С	It represents the amount of money Kevin and Molly spent respectively at Bookstore A.	B1
d	-2.2 + 1.5x = 5.3	
	x = 5	B1

26a	1.5 km/min	B1
Zua	1.5×1000	В
	$=\frac{1.5 \times 1000}{1 \times 60}$ =25 m/s	
b	Area = dist travelled	
		М1
	$21 = \frac{1}{2}(\nu + 1.5)(20)$	
	$21 = 10(\nu + 1.5)$	
	2.1 = v + 1.5	
	v = 0.6	A1
С	$\frac{speed - 0.6}{12} = \frac{1.5 - 0.6}{20}$	M1
	12 20	
	$\frac{speed - 0.6}{12} = 0.045$	
	12	
	speed = 1.14km / min	
	= 19m/s	A1
	OR	
:		
	$acc = \frac{1.5 - 0.6}{20} = 0.045$	
	speed = 0.6 + 12(0.045) = 1.14 km / min = 19m / s	
d	Area = dist travelled	
	$92.25 = \frac{1}{2}(0.6 + 1.5)(20) + 1.5(40) + \frac{1}{2}(t)(1.5)$	
		M1
	92.25 = 21 + 60 + 0.75t	
	11.25 = 0.75i	
	$t = 15 \min$	
	T is 0915	A1
27a	$\frac{BD}{2} = \frac{2}{2}$	
	3BD = 2DC DC 3	
	AD = AB + BD	
	$=\mathbf{m}+\frac{2}{5}\mathbf{B}\mathbf{C}$	
	5	
	$-m+\frac{2}{2}(-m+n)$	M1
	$=\mathbf{m}+\frac{2}{5}(-\mathbf{m}+\mathbf{n})$	
	$=\frac{3}{5}\mathbf{m}+\frac{2}{5}\mathbf{n}$	A1
	5 5 5	
bi		
	<u> </u>	

	$AR = kAD = \frac{3}{5}k\mathbf{m} + \frac{2}{5}k\mathbf{n}$ $BR = BA + AR$	M1
	$=-m+\frac{3}{5}k\mathbf{m}+\frac{2}{5}k\mathbf{n}$	
	$= \left(\frac{3}{5}k - 1\right)\mathbf{m} + \frac{2}{5}k\mathbf{n}$	M1
		IVI I
	Since AC is parallel to BR and $\stackrel{\text{NNSSO}}{AC} = \mathbf{n}$	A1
	$\frac{3}{5}k - 1 = 0$ $k = \frac{5}{3}$	
bii	$\frac{\text{Area of triangle } ABD}{\text{Area of triangle } RBD} = \frac{AD}{DR}$	
	$\frac{3}{2}$	A1

### **Broadrick Secondary School**

## 4E5N Preliminary Examination 2024

# Paper 2 Marking Scheme

1a	4.2×10 <sup>6</sup>	B1
b	$\frac{4.2 \times 10^6 - 3.6 \times 10^6}{3.6 \times 10^6} \times 100\%$	M1
	${3.6\times10^6}$ × 100%	
	$= \frac{16\frac{2}{3}\%}{3}$	A1
	= 3	
С	$\frac{3.6 \times 10^6}{100 - 4} \times 100\%$	M1
ľ	100 – 4 = 3750000	
	$=3.75\times10^6$	A1
2a	$12x - 8x^2 = 6 - 8x^2$	M1
: : 	12x = 6	
		A1
	$x = \frac{1}{2}$	A1
b	$x = \frac{1}{2}$ $1 - 3p \ge 5$	
	$-3p \ge 4$	
İ	$n \leq -\frac{4}{3}$	B1
	$p = \frac{3}{3}$	<u> </u>
С	$-3p \ge 4$ $p \le -\frac{4}{3}$ $3A = \frac{Ap + h}{1 - h}$	
  -	3A(1-h) = Ap + h	M1 (make
I	3A(1-h) = Ap + h $3A - 3Ah = Ap + h$	linear)
I	3A - 3Ah = Ap + h $3A - 3Ah - Ap = h$	
l	A(3-3h-p)=h	M1 (Factorise)
I	A(3-3n-p)=n	Wit (Facionse)
1	$A = \frac{h}{3 - 3h - p}$	A1
d	*	
		M1 (combine)
		RAA (assaura)
		M1 (expand)

	x 3 2	
	$\frac{x}{(x-4)^2} - \frac{3}{4-x} = 2$	M1 (quadratia
	$\frac{x}{(x-4)^2} + \frac{3}{x-4} = 2$	M1 (quadratic formula using
	( )	their found
	$\frac{x+3(x-4)}{(x-4)^2} = 2$	eqn)
	$x+3x-12=2(x^2-8x+16)$	A1
	$.4x - 12 = 2x^2 - 16x + 32$	
!	$0 = 2x^2 - 20x + 44$	
	$0 = x^2 - 10x + 22$	<u> </u>
	$x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(1)(22)}}{2(1)}$ $= \frac{10 \pm \sqrt{12}}{2}$	
	$10\pm\sqrt{12}$	
	= 6.73 or 3.27 (2dp)	
3a	3y + 5x - 6 = 0	
	$y = -\frac{5}{3}x + 2$	M1 (find m)
	$-1 = -\frac{5}{3}(-3) + c$ $c = -6$ $y = -\frac{5}{3}x - 6$	M1
	c = -6	
	$y = -\frac{5}{3}x - 6$	A1
b	$y = -\frac{5}{3}(0) - 6 = -6$	
	B(0,-6)	
	9+-6	
	Mid point of BD = $(0, \frac{9+-6}{2}) = (0, 1.5)$	M1 (find y value of C)
	C is (x, 1.5) and sub into $y = 7.5 - x$ 1.5 = 7.5 - x	
	x=6	
	So C is (6, 1.5)	A1
С	So C is (6, 1.5)  Area = $\frac{1}{2}$ (15)(3) + $\frac{1}{2}$ (15)(6)	M1 A1 (EGE from
	Area = 2 2 2 2	

	=67.5	(b))
d	Let <i>P</i> be (0,-1).	
	$\tan \angle ABP = \frac{3}{5}$	M1
!		IVI I
	$\angle ABP = \tan^{-1}\left(\frac{3}{5}\right)$	
	Let $Q$ be $(0,1.5)$ .	
	$\tan \angle CBQ = \frac{6}{7.5}$	M1
	7.3	
	$\angle CBQ = \tan^{-1}\left(\frac{6}{7.5}\right)$	
	$\angle ABC = \tan^{-1}\left(\frac{3}{5}\right) + \tan^{-1}\left(\frac{6}{75}\right)$	
	= 69.6° (7.5)	
	09.0	A1
	Or find langth of AD DC and AC and the section is	
4a	Or find length of AB, BC and AC and use cosine rule.	B1
bi	$X = pn^2 + qn$	
	When $n = 4$ and $X=2$ ,	
	$2 = p(4)^2 + q(4)$	
	2 = 16p + 4q	A1
	When $n = 5$ and $X=5$ ,	
	$5 = p(5)^2 + q(5)$	
	5 = 25p + 5q	A1
bii	16p + 4q = 2	
	80p + 20q = 10 (1)	
	25p + 5q = 5	
	100p + 20q = 20 (2)	
	(2)-(1)	M <sub>1</sub>
	20p = 10	
	p = 0.5	A1 A1
L::	q = -1.5	
bili		M1

	$495 = 0.5n^2 - 1.5n$	
	$0 = -495 - 1.5n + 0.5n^2$	M1
	$0 = n^2 - 3n - 990$	
	(n-33)(n+30) = 0	
	n = 33 or $n = -30$ (rej)	A1
	Since number of vertices is an integer, it is possible to have a <i>n</i> -sided polygon with 495 diagonals.	
5ai	$\angle ABC = \frac{100}{2} = 50^{\circ}$ (angle at centre = 2x angle at circumference)	B1
aii	$\angle ADC = 180^{\circ} - 50^{\circ} = 130^{\circ}$ (angles in opp seg)	B1
aiii	$\angle ACO = \frac{180^{\circ} - 100^{\circ}}{2} = 40^{\circ}$ (base angles of isos triangle)	M1
	$\angle ACO = {2} = 40$ (base angles of isos triangle)	
	$\angle COT = 40^{\circ}$ (alt angles, AC//OT)	M1
	$\angle OCT = 90^{\circ}$ (tan perpendicular to rad)	A1
<u> </u>	$\angle OTC = 180^{\circ} - 90^{\circ} - 40^{\circ} = 50^{\circ}$ (angle sum of triangle) $\angle ADC + \angle AOC = 130^{\circ} + 100^{\circ}$	· · · · · · · · · · · · · · · · · · ·
b		B1
	= 230°	-
	≠ 180°	
	They are not angles in opposite segment.  A circle cannot be drawn passing through the points A,	
	O, C and D.	
С		
	$\tan 50^\circ = \frac{OC}{4.8}$	M1
	OC = 5.72042	
	Minor segment = minor sector – triangle	
	$= \frac{100}{360} \times \pi (5.72042)^2 - \frac{1}{2} (5.72042)^2 \sin(100^\circ)$	М1
		A1
	=12.4 cm <sup>2</sup>	D1
6a	-3.33 (2dp)	B1 P2
6b	All points plotted correctly	C1
Goi	Smooth curve Tangent drawn such that it passes through (-1,2) and	C1
6ci	touches curve at 1 point and gradient is negative.	
6cii	$m = \frac{2 - (-1)}{-1 - 0} = -3$	M1
	c = -1	
	$\begin{cases} z = -1 \\ y = -3x - 1 \end{cases}$	A1
6d		
		<u> </u>

		r**
	$\frac{1}{x-1} - \frac{1}{4}x = 0$ $\frac{1}{x-1} - \frac{1}{4}x + \frac{5}{4}x - 1 = \frac{5}{4}x - 1$	M1
	$\begin{vmatrix} x-1 & 4 & 4 & 4 \\ y = \frac{5}{4}x - 1 & & & \end{vmatrix}$	M1
	Draw line on graph	A1
	x = <u>2.6</u> and <u>-1.5</u> (accept 2.5, 2.55) (accept -1.4, -1.45, -1.55, -1.6)	
7ai	Median = 353 g	B1
aii	UQ: 366 or 367	
J 4.11	LQ: 342 or 343	
1	IQR = 366-342	М1
	= 24g (also accept 23 or 25 g depending on their UQ &	A1
	LQ)	
b	20%>32 apples	M1
	Read at 128th apple	
	Min mass = 370 g	A1
С	14 160-104	M1
	$\frac{14}{160} \times \frac{160 - 104}{159} \times 2$	
	= 0.0616	A1
d	False. The first quartile which represents 25% of the apples are less than 320g. The upper quartile which represents 75% of the apples are less than 360g which implies that 25% of the apples are more than 360g  Hence there are equal number of apples weighing less than 320g and more than 360g.	B1 (states that the whiskers rep 25% of the data)
е	I disagree.	
	The median mass of apples from tree A is the same as that from tree B. On average, apples from tree A and B weigh the same.	B1
	IQR (Tree B) = 360 – 320 = 40g However, the interquartile range of the masses of the apples from tree B is bigger than that from tree A. The masses of the apples from tree B have a bigger spread, thus are less consistent.	B1

8a	$BE = \sqrt{15^2 + 8^2}$	M1
	= 17 cm	A1
b	$AG = \sqrt{17^2 + 10^2} = \sqrt{389}$	M1
	= 19.7 cm (3sf)	A1
С	Let <i>M</i> be the midpoint of <i>CG</i> and <i>N</i> be the midpoint of <i>BF</i> . $JM = \sqrt{8^2 - 4^2} = \sqrt{48}$	M1 M1
	Then $JN = 10 + \sqrt{48}$ $AN = \sqrt{15^2 + 4^2} = \sqrt{241}$	M1
	$AJ^{2} = (\sqrt{241})^{2} + (10 + \sqrt{48})^{2}$ $AJ = 22.96876$	A1
	= 22.97 (4sf) (shown)	-
d	$\cos \angle JAG = \frac{22.97^2 + \left(\sqrt{389}\right)^2 - 8^2}{2 \times 22.97 \times \sqrt{389}}$	M1
	$\angle JAG = 19.7796 = 19.8^{\circ} \text{ (1dp)}$ If use exact value, angle = 19.78165 = 19.8° (1dp)	A1
9a	Capacity = $\frac{1}{3}\pi(2)^2(3) + \frac{2}{3}\pi(3)^3$ =69.1150 = 69.1 m <sup>3</sup>	M1 A1
b	Curved hemisphere = $2\pi(3)^2 = 18\pi$ Ring = $\pi(3)^2 - \pi(2)^2 = 5\pi$	M1 (Hemisphere or ring)
	Slant height of cone, L = $\sqrt{2^2 + 3^2} = \sqrt{13}$ Curved area of big cone = $\pi(2)\sqrt{13} = 2\pi\sqrt{13}$	M1 (CSA of big cone using their L)
	Using similar solids,	
	$\frac{h_{\text{small cone}}}{h_{\text{big cone}}} = \sqrt[3]{\frac{1}{10}}$ $\frac{A_{\text{small cone}}}{A_{\text{big cone}}} = \left(\sqrt[3]{\frac{1}{10}}\right)^2 = \frac{1}{\sqrt[3]{100}}$	M1 (find ratio of h and then area)
	$\frac{A_{\text{contact with water}}}{A_{\text{big cone}}} = \frac{\sqrt[3]{100} - 1}{\sqrt[3]{100}}$ $A_{\text{contact with water}} = \frac{\sqrt[3]{100} - 1}{\sqrt[3]{100}} \times 2\pi \sqrt{13} = 17.7736$	M1 (find area
	Total area in contact = $18\pi + 5\pi + 17.7736$	of cone in contact)

	= 90.0302 = 90.0 m <sup>2</sup>					:	
		A1					
10a	$\frac{300}{1200} \times 100$	B1					
b	6+1.8×2×	< 49 = \$	3182.40			M1, A1	
С	<del>                                      </del>						
	Item		Description		Total cost	]	
	Printing of T-shirts		Double side (Bundle of 500 pcs)		\$7000 x 2= \$14000	M1 (T-shirt printing)	
	Goodie Bags		No of packs req = 1000/5 = 200				
			Bulk price (100+ packs)		\$18 x 200 = \$3600	M1 (bag)	
	Booking venue			dvance	\$1200		
	Refreshments		Large set  Regular set		\$3 x 1000 = \$3000 or		
					\$2.80 x 1000 = \$2800		
			Small set		or \$2.50 x 1000 = \$2500	M1 (medals)	
	Participan medals	ts	Number of pack of 50 = 1000/50 = 20		\$210 x 20 = \$4200		
	Total weig	M1 (shipping)					
	Local Courier	Numb	per of parcels	Cost			
	Simply	140		$(4.80+1.85\times2\times79)$			
	Post	-	$\frac{10}{80} \approx 2$	$+(4.80+1.85\times2\times59) = 520.20$			
			cel of 80 kg + rcel of 60 kg				
	Singapor e Post	$\frac{140}{2} \approx 3$		$2(6+1.80\times2\times49)$			
	8 FUSI	50		$+(6+1.80\times2\times39)$			
			els of 50 kg + rcel of 40 kg	= 511.20			
	DPEX	140 ≈ 5		$4(5.5+1.60\times2\times29)$			
		30		$+(5.5+1.60\times2\times19)$			
			els of 30 kg + rcel of 20 kg	= 727.60			
	Choose S	M4 (anat after					
	Total costs after GST =					M1 (cost after GST)	
	(14000 + 3	600+1	200+3000+4	4200 + 511	$.20) \times \frac{109}{100}$		

=28	89	7.	20	8
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At least 40% to charity, so 60% will be to cover costs:

Including charity =  $\frac{28897.208 \times \frac{100}{60}}{200} = 48162.01$ 

M1 (total including charity)

Fee for each participant=  $\frac{48162.01}{1000} = $48.16$ 

**A**1

To donate at least 60% of the proceeds and cover all costs, sensible amount to charge each participant = \$50.