Name:	Class:	Class Register Number:



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CHUNG CHENG HIGH SCHOOL (MAIN)

Chung Cheng High School Chung

# PRELIMINARY EXAMINATION 2024 SECONDARY 4

## **MATHEMATICS**

4052/01

Paper 1

Friday 23 August 2024 2 hours 15 minutes

Candidates answer on the Question Paper.

#### **READ THESE INSTRUCTIONS FIRST**

Write your name, class and index number on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

Answer all the questions.

The number of marks is given in brackets [ ] at the end of each question or part question.

If working is needed for any question, it must be shown with the answer.

Omission of essential working will result in loss of marks.

The total of the marks for this paper is 90.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

For Exan	niner's Use
Total	/ 90

## Mathematical Formulae

Compound interest

Total amount = 
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone =  $\pi r l$ 

Surface area of a sphere =  $4 \pi r^2$ 

Volume of a cone = 
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere = 
$$\frac{4}{3} \pi r^3$$

Area of triangle 
$$ABC = \frac{1}{2}ab\sin C$$

Arc length =  $r\theta$ , where  $\theta$  is in radians

Sector area = 
$$\frac{1}{2}r^2\theta$$
, where  $\theta$  is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$Mean = \frac{\sum f x}{\sum f}$$

Standard deviation = 
$$\sqrt{\frac{\sum f x^2}{\sum f} - \left(\frac{\sum f x}{\sum f}\right)^2}$$

# Answer all the questions.

Answer:
Given that $0 < x < 180$ , find the possible values of x for $\sin x^{\circ} = 0.985$ . Give your answers correct to 1 decimal place.
$Answer x = \dots \text{or} \dots \text{[2]}$
(a) Simplify $\frac{(4a^4b)^3}{10a^3b^7}$ , leaving your answer in positive index form.
Answer[2]
<b>b)</b> Given that $2^x = 3$ , $2^y = 7$ and $2^z = \frac{9}{49}$ , use the laws of indices to find the value of $2^{3x-y+\frac{1}{2}z}$ .
· ·

Answer .....

[2]

4	lefto \$296	oup of students won \$226 in a competition and shared the amount equally, leaving \$4 ver. Competing for a second time, the same group of students won \$296. They shared the salong with the \$4 left over from the first competition equally, with no amount remaining. It is that each student received a whole number of dollars in both distributions, find the test possible number of students in the group.
		<i>Answer</i> students [2]
5	(a)	On 6 June 2020, Elijah invested some money in a bank which pays a simple interest at a rate of 3.5% per annum. He received a total interest of \$680.40 on 6 June 2023.  Find the amount of money Elijah invested in the bank.
	(b)	Answer \$
		Answer \$ [2]

BP~205

Diagram 1

Diagram 2

Diagram 3

Diagram 5

From the diagrams above, select one of them which best illustrates each of the following statements.

- (a)  $y = 4\pi x^3$ .
- (b) The cost of a project \$y\$ is a linear function of x, where x is the number of man-hours required to complete the project. The project has a fixed cost of \$100.
- (c) An object is travelling at a constant speed towards a fixed point O. The distance y (in metres) represents how far the object is from point O at time x (in minutes).
  - Answer (a) Diagram ......[1]
    - (b) Diagram ......[1]
    - (c) Diagram ......[1]
- 7 Write as a single fraction in its simplest form  $\frac{4-x}{x+2} \frac{2}{3-x}$

Answer ......[2]

6

8 The table shows the distribution of the weights of 40 students.

Weight (Wkg)	$40 < W \le 50$	$50 < W \le 60$	$60 < W \le 70$	$70 < W \le 80$	$80 < W \le 90$
Frequency	6	8	а	11	3

(a)	Find	the	value	of	a.
-----	------	-----	-------	----	----

		Answer a =[1]
(b)	Calculate an estimate for  (i) the mean weight of the students,	
	(ii) the standard deviation of the weights.	Answerkg [1]
		Answerkg [1]
(c)	An error in the weighing machine caused the str	idents' weights to be recorded 2 kg more
	than their actual values.	
	Explain how the mean and standard deviation w	ill change after the error is rectified.
	Answer	
	,	

	<i>,</i>
9	Andy bought a limited-edition watch from an online website based in Thailand for 10 460 baht.
	Andy also paid \$15 in Singapore dollars for shipping and GST of 9% on the cost of the watch.
	The exchange rate between Thai baht (B) and Singapore dollars (SS) was \$100=SSP.
	Andy spent a total of \$436 in Singapore dollars.
	Find the value of P, giving your answer correct to 3 significant figures.

Answer	<i>P</i> =	[3]
		1-1

10 The gradient of the line joining the points (-3+2a,7) and (a+1,2) is  $-\frac{2}{3}$ . Find the value of a.

11 Given that  $a^2 - \frac{6a}{b} + \frac{9}{b^2} = 0$ , find the value of ab.

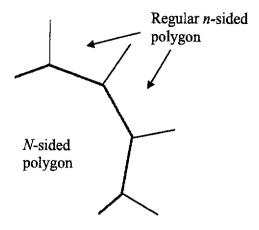
				G
12	Factorise completely	$4mn-16n^2$	$-4m^2n+6$	$54n^3$

Answer[3	3	]	
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- 13 A bag contains 4 black coins, 7 red coins and 11 white coins. Two coins are drawn from the bag at random, one after another without replacement.
  - (a) Find the probability that a white coin will be chosen on the second draw.

(b) x yellow coins are added to the bag. The probability of picking a black coin in **both** draws is  $\frac{1}{50}$ . Find the value of x.

14 A number of regular *n*-sided polygons are placed together in a ring to form a regular *N*-sided polygon as shown in the diagram below.



(a) Show that 
$$N = \frac{2n}{n-4}$$
.

[3]

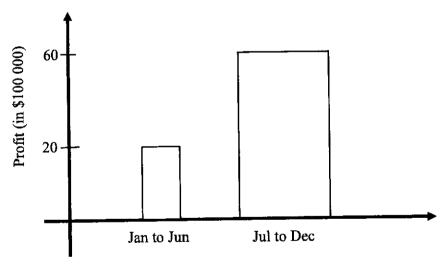
(b) Hence, explain why a regular octagon cannot be formed by placing smaller n-sided regular polygons in a ring.

Answer

15 (a) Express  $x^2 + 5x + 7$  in the form  $(x+a)^2 + b$ .

	Answer[2]
(b)	Hence, explain why the expression will never be negative.
	Answer
	[1]

16 A company presented their 2023 financial report in this graph.

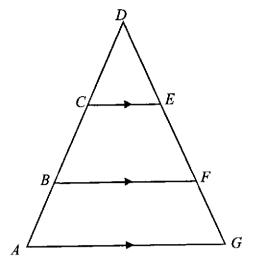


State one aspect of the graph that may be misleading and explain how they may lead to a misinterpretation.

Ans	swer	
	•••••	[2]

{i	ε = ·	ε =	= {:	inte	ger x	: (	0 < x	≤12	}																			
							bers}																					
$B = \{\text{numbers that have at least 2 distinct factors}\}$																												
Е	(a)	(a)	I	Expl	ain v	vhy	y A is	a p	горе	er si	ubs	et o	of <i>B</i>	wit	thou	ut li	isti	ng (	dov	vn tl	ne e	lem	ents.					
A			A	4nsv	ver																							
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D	<b>(b)</b>	(b)	Ι	Draw	a V	'en	n dia	gran	n ar	ıd li	ist (	dow	n th	ie e	len	nen	ts t	o il	lus	trate	the	abo	ve ii	ıforn	nation	n.		
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18 The diagram shows a triangle AGD with the points C and B lying on AD and points E and F lying on GD.



It is given that CE//BF//AG, BF = 2CE and AG = 3CE.

(a) Show that triangle DCE is similar to triangle DBF.

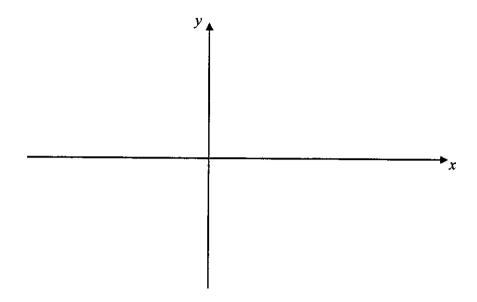
Answer

[2]

(b) Given that the area of trapezium  $BFEC = 15 \text{ cm}^2$ , find the area of trapezium AGFB.

Answer ......cm<sup>2</sup> [3]

19 Sketch the graph of y = (2+x)(x-6) on the axes below. Indicate clearly the values where the graph crosses the axes and write down the equation of the line of symmetry.



Answer line of symmetry: ......[3]

20 It is given that y is inversely proportional to the square root of x. Find the percentage change in x when the value of y decreases by 50%.

Answer ......[2]

21 The table shows the prices of movie tickets categorised by different days of the week and the various age groups.

	Monday to Thursday	Friday	Saturday and Sunday
Child	\$6.00	\$8.50	\$9.00
Adult	\$7.00	\$10.00	\$12.50
Senior Citizen	\$6.50	\$9.00	\$10.00

	Adult	\$7.00	\$10.00	Ψ12.50			
Ser	nior Citizen	\$6.50	\$9.00	\$10.00			
a) Write	e down a 3×3 mar	trix P to represent the	above information.				
~,		-					
			Answer <b>P</b> =	[1			
		2	2,,5,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	μ			
	TEL NI Comillo	iono a abild to	wo adults and a senior	r citizen while the Ta			
b) (i)	The Ng Tamily	comprises a ciniu, iv	trro adulta Danrasan	t this information as			
		s three children and	two adults. Represen	t tins information as			
	$2\times3$ matrix <b>Q</b> .						
			Answer <b>Q</b> =	[			
(ii)	Evaluate QP and	d explain what the eler	ments represent.				
( )		-					
	Answer						
	*14***********		*************************				
		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,					
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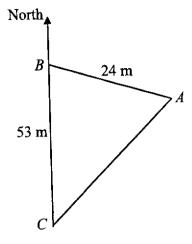
22 Sam's daily morning routine involves getting breakfast before going to work. He travels by car. On a particular day, Sam leaves home at 8:00 am and arrives at the breakfast place at 8:15 am. He leaves the breakfast place at 8:30 am. He arrives at his office at 9:00 am. Sam's average speed for the whole journey is 42 km/h.

His average speed from home to the breakfast place is 10 km/h faster than his average speed from the breakfast place to the office.

Find the distance between the breakfast place and Sam's office.

Answer	 	 	km [4]

23 Three points A, B and C lie on a horizontal ground are such that AB = 24 m and BC = 53 m. Point B is due north of C. The bearing of A from B is  $122^{\circ}$ .



(a) Find the distance AC.

Answer m [2	2
-------------	---

(b) Find the bearing of C from A.

(c) Find the area of the triangular plot ABC.

17

					•
24	The first four	terms in a	sequence of	f numbers	are

$$3+k,1+k,-1+k,-3+k,...$$

where k is a constant.

(a) Find an expression in terms of n and k, for the nth term in this sequence.

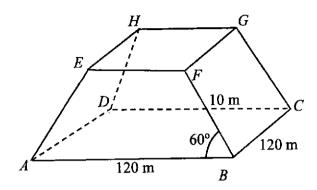
Answer ......[1]

(b) State two conditions on k such that 39 is a term of the sequence.

Answer

[2]

25 The diagram below shows an indoor adventure park in the shape of a trapezoidal prism with a square base *ABCD*. The indoor adventure park is positioned on horizontal ground and the walls *ADHE* and *BCGF* are slanted.



The top of the prism, EFGH, is the ceiling of the adventure park which is also horizontal. EFGH is a square and the centre of EFGH lies vertically above the centre of ABCD. AB = 120 m, AE = BF = CG = DH = 10 m and  $\angle ABF = 60^{\circ}$ .

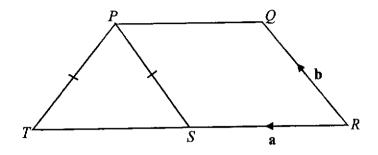
(a) Find the area of ABFE.

	m <sup>2</sup>	Γ <b>/</b> 1
Answer		[4]

(b) The owner of the indoor park wants to build a flying fox feature from point H to point B. The angle of depression from point H to point B must not exceed  $5^{\circ}$ , in order to meet the safety requirements. Explain, with mathematical working, whether the flying fox feature can be built.

Answer

26 In the diagram below, PQRST is a trapezium made up of a parallelogram PQRS and an isosceles triangle PST where PT = PS. It is given that  $\overline{RS} = \mathbf{a}$ ,  $\overline{RQ} = \mathbf{b}$  and SR = ST.



(a) Show that  $\overrightarrow{QS} = \overrightarrow{PT}$ .

Answer

[2]

(b) Hence or otherwise, prove that the trapezium is made up of three isosceles triangles *PST*.

Answer

Name:	Class:	Class Register Number:



Chung Cheng High School Chung

# PRELIMINARY EXAMINATION 2024 SECONDARY 4

## **MATHEMATICS**

4052/02

Paper 2

Tuesday 20 August 2024 2 hours 15 minutes

Candidates answer on the Question Paper

### **READ THESE INSTRUCTIONS FIRST**

Write your name, class and index number in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs. Do not use paper clips, glue or correction fluid.

Answer all questions.

The number of marks is given in brackets [ ] at the end of each question or part question.

If working is needed for any question it must be shown with the answer. Omission of essential working will result in loss of marks. The total number of marks for this paper is 90.

The use of an approved scientific calculator is expected, where appropriate. If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

For Examiner's Use				
Question Number	Marks Obtained			
1				
2				
3				
4				
5				
6				
7				
8				
9				
Total Marks				

This document consists of 23 printed pages and 1 blank page.

### Mathematical Formulae

Compound interest

Total amount = 
$$P\left(1 + \frac{r}{100}\right)^n$$

Mensuration

Curved surface area of a cone =  $\pi r l$ 

Surface area of a sphere =  $4 \pi r^2$ 

Volume of a cone = 
$$\frac{1}{3}\pi r^2 h$$

Volume of a sphere = 
$$\frac{4}{3}\pi r^3$$

Area of triangle 
$$ABC = \frac{1}{2}ab\sin C$$

Arc length =  $r \theta$ , where  $\theta$  is in radian

Sector area = 
$$\frac{1}{2}r^2\theta$$
, where  $\theta$  is in radian

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc\cos A$$

Statistics

$$Mean = \frac{\Sigma fx}{\Sigma f}$$

Standard deviation = 
$$\sqrt{\frac{\Sigma f x^2}{\Sigma f} - \left(\frac{\Sigma f x}{\Sigma f}\right)^2}$$

**TURN OVER FOR QUESTION 1** 

1 (a) The table shows the total electricity consumption in Singapore over three years.

Year	2020	2021	2022
Total Electricity Consumption in Gigawatt Hours (GWh)	50 779	53 483	54 884

(i)	In 2021, the electricity consumed by households took up 15.5% of the total
`	electricity consumption. Calculate the amount of electricity consumed by
	households in 2021, correct to two significant figures.

Answer		GWh	[1]
--------	--	-----	-----

(ii) Calculate the percentage increase in the total electricity consumption from 2020 to 2022.

(iii) Express the 2020 electricity consumption in kilowatt hours (kWh), leaving your answer in standard form, correct to two significant figures.

		5
(b)	A m	icroprocessor is in the shape of a cube where the sides are 5 mm in length.
	(i)	Find the maximum number of microprocessors that can be placed into a container with dimensions 10 cm by 2 cm by 8 cm.
		Answer [2]
	(ii)	A model of the microprocessor was made to a scale of 10:1. Given that the surface area of microprocessor is 150 mm <sup>2</sup> , find the surface area of the model microprocessor in square centimetres.
		Answer cm <sup>2</sup> [2]

2 (a) Solve $2x-7=3(1-3x)$	2	(a)	Solve	2x-7 = -7	=3(1-3x)
----------------------------	---	-----	-------	-----------	----------

Answer 
$$x = \dots [2]$$

**(b)** Solve the inequalities 7x-1<13 and  $\frac{x+1}{2} \ge -2(x-2)$ .

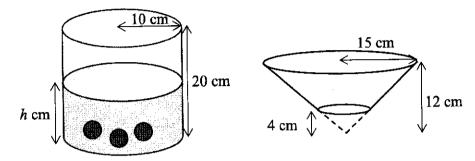
(c) Rearrange the formula  $y = \frac{x^2 + 5}{7x^2}$  to make x the subject.

(d) Solve the equation  $\frac{2x}{1-x} - 3 = \frac{1}{2x-3}$ .

Give your solutions correct to two decimal places.

The diagram shows two open containers, a right cylinder and an inverted frustum. The right cylinder has a base radius of 10 cm and a height of 20 cm. The frustum is formed by cutting a smaller cone off the bottom of a larger cone. The smaller cone that was cut off has a height of 4 cm. The larger cone has a base radius of 15 cm and a height of 12 cm.

Three identical spherical marbles, each of radius 3 cm, are placed into the cylindrical container and water is poured in to a depth of h cm.



(a) Find the volume of each marble, leaving your answer in terms of  $\pi$ .

Answer	***************************************	$cm^3$	[1]
--------	---	--------	-----

(b) Find the volume of the frustum, leaving your answer in terms of  $\pi$ .

(c)	All the water from the cylinder, without the marbles, is then poured into the empty frustum, filling it completely without any overflow.
	Find the value of $h$ , correct to two decimal places.
	Answer $h = \dots $ [3]
(d)	The exterior surface area of each container is painted.
	Find the total area painted.

Answer ..... cm<sup>2</sup> [6]

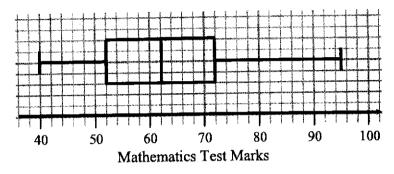
[Turn over

4 (a) 12 students from class A took a Mathematics test.

The table below shows the test marks of the students. However, two of the students' marks are covered with ink.

40	95	84	47	63
52	63	55	52	61
		·		

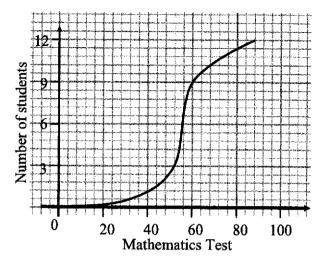
(i) Given that the box-and-whisker plot below shows the distribution of the results, explain why the information may not be sufficient to find the missing marks of the two students.



Answer	
	 [1]

(ii) Given further that the modal mark is 63, find the two missing marks.

(iii) 12 students from class B also took the same Mathematics test. The distribution of their test marks is shown on the cumulative frequency graph.



Make a comment comparing the averages and a comment comparing the distribution of the Mathematics Test marks between the two classes.

Use figures to support your answers.

Answer						
• • • • • • • •			• • • • • • • • • • • • • • • • • • • •			************
•••••	• • • • • • • • • • •			•••••	•••••••	
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• • • • • • • • •	• • • • • • • • • • • •	• • • • • • • • • • • • • • • •			• • • • • • • • • • • • • • • •	[3]

(b) Alice rolled a six-sided die, X, 100 times. Bala rolled another six-sided die, Y, 80 times. The number of times they each obtained a '6' is recorded in the table.

Die	Number of rolls	Number of times '6' is obtained
X	100	16
Y	80	18

(i) Find the probability of rolling a '6' by Alice and Bala respectively.

(ii) One of the dice is biased. Using your answers in (b)(i), determine which die, X or Y, is likely to be the unbiased 6-sided die. Explain your answer.
Answer

······································	•••••

......[1]

2024 Preliminary Exam/CCHMS/Secondary 4/Mathematics/4052/02

[Turn over

5 (a) Complete the table of values for  $y = \frac{2}{x^2} - 2x$ .

Values are given to one decimal place where appropriate.

$\begin{array}{ c c c c c c c c c c c c c c c c c c c$											
31 45 4 9 13.3 7 0 -3.5 -5.8	Γ		_3	-2.	-1	-0.5	-0.4	0.5	1	2	3
	ŀ	1/		4.5	4	9	13.3	7	0	-3.5	-5.8

[1]

- **(b)** On the grid opposite, draw the graph of  $y = \frac{2}{x^2} 2x$  for  $-3 \le x \le 3$ . [3]
- (c) (i) On the same grid, draw the graph of y + x = 6 for  $-3 \le x \le 3$ .

[1]

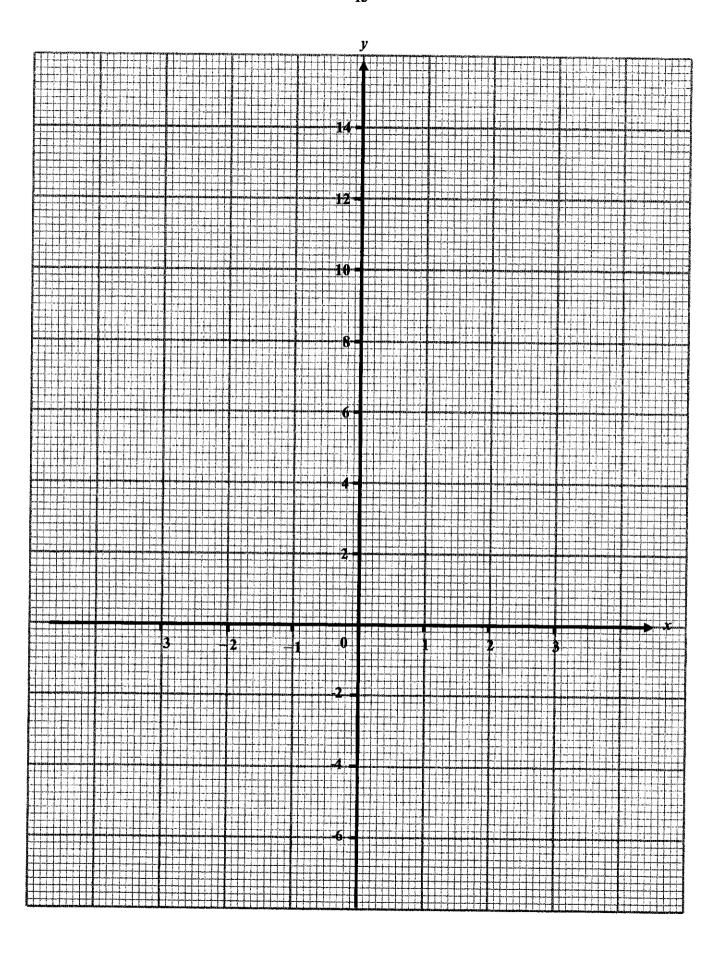
(ii) Write down the x-coordinates of the points where the line intersects the curve.

Answer x = ..... and ..... [2]

(iii) These values of x are solutions of the equation  $x^3 + Ax^2 + B = 0$ . Find the value of A and of B.

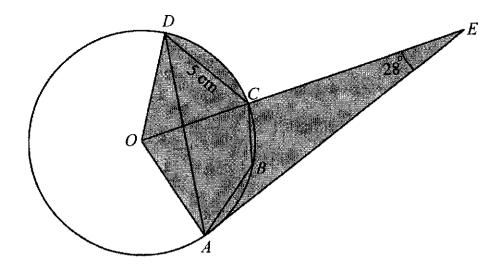
Answer A = .....

*B* = .....



14

6



A, B, C and D are points on the circle with centre O and radius 5 cm. AE is a tangent to the circle at A and OE is a straight line that passes through C. Angle  $OEA = 28^{\circ}$  and CD = 5 cm.

- (a) Find, giving a reason for each step of your working,
  - (i) angle OAD,

Answer Angle 
$$OAD = \dots ^{\circ} [3]$$

(ii) angle ABC.

(b) Find the area of the shaded region.

Answer ...... cm<sup>2</sup> [4]

- 7 (a) A, B, C and D are four points such that the coordinates of A and C are (4,2) and (10,-34) respectively.  $\overline{AB} = \begin{pmatrix} -9 \\ -12 \end{pmatrix}$  and  $\overline{AD} = \begin{pmatrix} 24 \\ -12 \end{pmatrix}$ .
  - (i) Find the coordinates of B.

Answer	( , )	[1]
2111011101	( , ,	, r

(ii) Find  $|\overrightarrow{AB}|$ .

Answer 
$$|\overrightarrow{AB}| = \dots$$
 units [1]

It is given that E is a point on BD such that  $\overrightarrow{BE} = \frac{1}{3}\overrightarrow{BD}$ .

(iii) Show that A, C and E are collinear. Answer

))		the point $(2,6)$ , $B$ is the point $(-4,-2)$ ugh point $C$ and is parallel to $AB$ .	and C is the point $(6, -2)$ . A line L pass	ies
	(i)	Find the equation of line $L$ .		
			Answer [	[2]
	Poin	t D lies on line L such that $AD//BC$ .		1
	(ii)	Find the coordinates of point D.		
			Answer D ( )	[2]
	(iii)	Show that <i>ABCD</i> is a rhombus.		
		Answer		

8	(a)	The fi	gure shov	ws the first three fig	ures of a seque	nce formed by	sticks of the same size.
			Figure 1	Figures form		Figures is rec	
				Figure Number	Number o	of Squares	
				1		$()^2-1$	
				2	(2+1	$\left(-1\right)^{2}-1$	
				3	(3+1	$(1)^2 - 1$ $(1)^2 - 1$	
		(i) (ii)		number of small sq terms of $n$ , an expre	Answ	er	[1] es in Figure <i>n</i> .
					Answ	er	[1]
		(iii)	Explain odd.	why the sum of the	number of squa	ares in two cons	secutive figures is always
			Answer				
						*************	[2

**(b)** The table below shows the  $n^{th}$  terms of 4 sequences.

Sequence number	n <sup>th</sup> term
1	4n + 3
2	7n + 1
3	14n
4	8 <i>n</i> – 1

For each sequence, are the numbers in the sequence always multiples of 7, sometimes multiples of 7 or never multiples of 7?

Write down the letter 'A', 'S' or 'N' to represent your answer.

- A Always multiples of 7
- S Sometimes multiples of 7
- N Never multiples of 7

Answer	
Sequence 1	
Sequence 2	
Sequence 3	
Sequence 4	[2]

Sam is a 40-year-old man who earns a gross salary of \$8000 a month. He is a Singaporean and an employee of a Singapore firm. Sam is required to put a certain percentage of his monthly gross salary into his Central Provident Fund (CPF) account.

CPF is a mandatory (social security) savings scheme funded by contributions from employers and employees. The table below shows the CPF contribution rates by employers and employees.

Employee's age	CPF Contribution Rates from 1 January 2024 (Monthly gross salary > \$750)							
(Years)	Total (% of gross salary)	By Employer (% of gross salary)	By Employee (% of gross salary)					
55 and below	37	17	20					
Above 55 to 60	31	15	16					
Above 60 to 65	22	11.5	10.5					
Above 65 to 70	16.5	9	7.5					
Above 70	12.5	7.5	5					

(a) Find the amount of money Sam's employer must contribute to his CPF monthly.

Answer \$.....[1]

Sam wants to plan his monthly savings and has tabulated his monthly expenditure as shown in the table. He hopes to save at least 20% of his salary each month after CPF deductions.

Expenditure	Amount (\$)
Food and Groceries	820
Transportation	90
Insurance and Healthcare	1000
Phone and Internet Subscriptions	80
Utilities	300
Housing Loan	1000
Leisure and Entertainment (movies, sports, books subscription fees, dining etc)	1580

(b)	Determine whether calculations.	Sam	is	able	to	achieve	his	saving	goals	by	clearly	showing	your
•••••	•••••••••••••••••••••••••••••••••••••••		•••	*****	• • • •		••••	••••••		• • • •	••••••	*********	••••
• • • • • • • • • • • • • • • • • • • •		• • • • • • •	•••	•••••	• • • •	••••••	••••	********	*****		,,,,,,,,,,	*******	. [4]

(c) After a year of saving, Sam decides to invest \$15 000 of his savings for a period of 5 years. He comes up with 2 investment plans.

## Plan A

Sam can invest his money in a 5-year savings bond at the beginning of 2025. The interest rate for the 5-year term is shown in the table. The savings bond compounds annually.

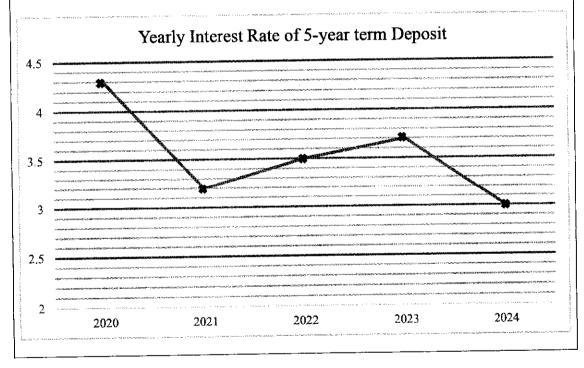
Year from issue date	1	2	3	4	5
Interest per year %	3.19	3.19	3.20	3.28	3.31

## Plan B

Sam can invest his money at the beginning of 2025 into an insurance company's fixed deposit account for a period of 5 years, compounded yearly. The interest rate is fixed over the duration of the investment and is determined by the year of issuance.

For example: If Sam had invested his money in 2020, over a period of 5 years, his investment plan would be at an interest of 4.3% compounded yearly over the period of 5 years.

However, the interest rate for 2025 is not yet available. Sam finds the information about the interest rates offered by the insurance company for the last 5 years.



23							
Determine which plan Sam should choose.							
Justify the decision you make and show your calculations clearly.							
***************************************							

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CHUNG CHENG HIGH SCHOOL (MAIN)

PRELIMINARY EXAMINATION 2024
SECONDARY 4

MATHEMATICS

Paper 1

Candidates answer on the Question Paper.

4052/01 Friday 23 August 2024

2 hours 15 minutes

MARKS SCHEME

This document consists of 20 printed pages.

Turn over

2024 Preliminary Exam/CCHMS/Secondary 4/Mathematics/4052/01

Class Register Number:

Mathematical Formulae

Total amount =  $P\left(1 + \frac{r}{100}\right)^n$ 

Compound interest

Mensuration

Curved surface area of a cone =  $\pi r l$ 

Surface area of a sphere =  $4 \pi r^2$ Volume of a cone =  $\frac{1}{3}\pi r^2 h$ 

Volume of a sphere =  $\frac{4}{3}\pi r^3$ 

Area of triangle  $ABC = \frac{1}{2}ab\sin C$ 

Arc length =  $r \theta$ , where  $\theta$  is in radians

Sector area =  $\frac{1}{2}r^2\theta$ , where  $\theta$  is in radians

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

 $a^2 = b^2 + c^2 - 2b \cos A$ 

Statistics

$$Mean = \frac{\sum f x}{\sum f}$$

Standard deviation =  $\sqrt{\frac{\sum f x^2}{\sum f}} - \left(\frac{\sum f x}{\sum f}\right)^{\frac{1}{2}}$ 

length to the width of the court in its simplest form. The length of a court is 0.028 km and the width of the court is 16 m. Express the ratio of the

28:16 7:4

Answer .....[1]

N Given that 0 < x < 180, find the possible values of x for  $\sin x^{\circ} = 0.985$ Give your answers correct to 1 decimal place.

$$\sin x^{\circ} = 0.985$$
  
 $x = \sin^{-1} 0.985 \text{ or } 180 - \sin^{-1} 0.985$   
 $= 80.1 \text{ or } 99.9$ 

Answer 
$$x = ......$$
 [2]

(a) Simplify  $\frac{(4a^4b)^3}{10a^3b^7}$ , leaving your answer in positive index form

نبا

$$\frac{\left(4a^4b\right)^3}{10a^3b^7} = \frac{64a^{12}b^3}{10a^3b^7}$$

$$= \frac{32a^9}{5b^4}$$

(b) Given that  $2^x = 3$ ,  $2^y = 7$  and  $2^z = \frac{9}{49}$ , use the laws of indices to find the value of  $2^{3x-y+\frac{1}{2}}$ 

Answer .....

[2]

$$2^{3\kappa^{-\gamma+\frac{1}{2}r}} = (2^{x})^{3} + 2^{y} \times (2^{z})^{\frac{1}{2}}$$

$$= 3^{3} + 7 \times \sqrt{\frac{9}{49}}$$

$$= \frac{81}{49}$$

$$= \frac{81}{49}$$
1:  $(a^{m})^{n} = a^{mn}$  to award M1 if student 3:  $a^{m} + a^{n} = a^{m+n}$  show understanding of 4:  $a^{\frac{1}{n}} = {}^{x} \sqrt{a}$  either law of indices

A group of students won \$226 in a competition and shared the amount equally, leaving \$4 leftover. Competing for a second time, the same group of students won \$296. They shared the \$296 along with the \$4 left over from the first competition equally, with no amount remaining.

greatest possible number of students in the group. Assuming that each student received a whole number of dollars in both distributions, find the

HCF is 6. There are 6 students.

Answer .....students [2]

Ų, (a) On 6 June 2020, Elijah invested some money in a bank which pays a simple interest at a rate of 3.5% per annum. He received a total interest of \$680.40 on 6 June 2023.

Find the amount of money Elijah invested in the bank

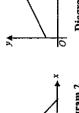
Amount of interest earn per year = \$680.40 ÷ 3

= \$226.80  
Amount of money invested = 
$$\frac{100}{3.5} \times $226.80$$
  
= \$6480

(b) Freddy invested \$8000 in another bank that paid compound interest at a rate of 1.75% per annum, compounded quarterly.

Find the total amount Freddy received at the end of 5 years. Give your answer correct to the

Total amount=
$$8000 \left(1 + \frac{1.75 + 4}{100}\right)^{5.4}$$
  
= \$8729.87 (nearest cent)



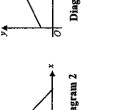


Diagram 3

From the diagrams above, select one of them which best illustrates each of the following statements.

Diagram 5

Diagram 4

- (a)  $y = 4\pi x^3$ .
- (b) The cost of a project \$y is a linear function of x, where x is the number of man-hours required to complete the project. The project has a fixed cost of \$100.
- (c) An object is travelling at a constant speed towards a fixed point O. The distance y (in metres) represents how far the object is from point O at time x (in minutes).

(c) Diagram ...2......[1]

7 Write as a single fraction in its simplest form  $\frac{4-x}{x+2} - \frac{2}{3-x}$ 

$$\frac{4-x}{x+2} - \frac{2}{3-x} = \frac{(4-x)(3-x)-2(x+2)}{(x+2)(3-x)}$$

$$-12-7x + x^2 - 2x - 4$$

$$=\frac{12-7x+x^2-2x-4}{(x+2)(3-x)}$$

$$=\frac{x^2-9x+8}{x^2-6x+8}$$

$$=\frac{(x+2)(3-x)}{(x-1)(x-8)}$$

$$=\frac{(x-1)(x-8)}{(x+2)(3-x)}$$

Answer .....[2]

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Tum over

The table shows the distribution of the weights of 40 students.

Weight (Wkg)	40 < W ≤ 50	50 < W ≤ 60	60 < 77 < 70	70 < 177 ≤ 80	06 ≥ 1⁄4 > 08
Frequency	y	٥	t	1.	·

(a) Find the value of a.

Answer a = 12 [1]

- (i) the mean weight of the students,
- Answer .....kg [1] (ii) the standard deviation of the weights.

Answer .....kg [1]

(c) An error in the weighing machine caused the students' weights to be recorded 2 kg more than their actual values.

Explain how the mean and standard deviation will change after the error is rectified.

Answer

The mean will decrease by 2kg to 62.25kg while the standard deviation remains unchanged. Ξ:

Find the value of P, giving your answer correct to 3 significant figures Andy spent a total of \$436 in Singapore dollars Andy also paid \$15 in Singapore dollars for shipping and GST of 9% on the cost of the watch Andy bought a limited-edition watch from an online website based in Thailand for 10 460 baht The exchange rate between Thai baht (B) and Singapore dollars (S\$) was \$100=S\$P

Cost of watch in Singapore dollars (without GST) =  $\frac{10460}{100} \times P$ =104.6P

Cost of watch in Singapore dollars (with GST) =  $1.09 \times 104.6P$ =114.014P

$$114.014P + 15 = 436$$
  
 $P = 3.69(3sf)$ 

The gradient of the line joining the points (-3+2a,7) and (a+1,2) is  $-\frac{2}{3}$ . Find the value of a.

10

gradient = 
$$\frac{2-7}{a+1-(-3+2a)}$$
  
=  $\frac{-5}{-a+4}$   
Given gradient =  $-\frac{2}{3}$ 

$$\frac{-5}{-a+4} = -\frac{2}{3}$$

$$-15 = -2(-a+4)$$

$$a = -\frac{7}{2}$$

11 Given that 
$$a^2 - \frac{6a}{b} + \frac{9}{b^2} = 0$$
, find the value of  $ab$ .

Answer  $a = \dots$ 

. [2]

$$a^{2} - \frac{6a}{b} + \frac{9}{b^{2}} = 0$$

$$a^{3} - 2a\left(\frac{3}{b}\right) + \frac{9}{b^{3}} = 0$$

$$\left(a - \frac{3}{b}\right)^{2} = 0$$

$$a - \frac{3}{b} = 0$$

$$a - \frac{3}{b} = 0$$

$$ab = 3$$

$$\begin{pmatrix} b \\ a - \frac{3}{b} = 0 \\ a = \frac{3}{b} \\ ab = 3 \end{pmatrix}$$

$$a = \frac{3}{b}$$

$$ab = 3$$

$$a - \frac{3}{b} = 0$$

$$a = \frac{3}{b}$$

$$ab = 3$$

$$a = \frac{3}{b}$$

$$ab = 3$$

 $Answer\ ab = \dots \qquad [2]$ 

12 Factorise completely  $4mn-16n^2-4m^2n+64n^3$ 

$$4mn-16n^2-4m^2n+64n^3=4n(m-4n)-4n(m^2-16n^2)$$

$$=4n(m-4n)-4n(m-4n)(m+4n)$$

$$=4n(m-4n)(1-m-4n)$$

13 A bag contains 4 black coins, 7 red coins and 11 white coins. Two coins are drawn from the bag

Answer ......[3]

at random, one after another without replacement.

(a) Find the probability that a white coin will be chosen on the second draw

Total number of coins = 4 + 7 + 11

P(second coin is white) = P(1st coin of any colours, 2nd coin is white)

(b) x yellow coins are added to the bag. The probability of picking a black coin in both draws is  $\frac{1}{50}$ . Find the value of x.

Total number of coins = 22 + x

P(both coins are black) = 
$$\frac{4}{22+x} \times \frac{3}{21+x}$$

$$\frac{12}{(22+x)(21+x)} = \frac{1}{50}$$

$$600 = (22+x)(21+x)$$

$$600 = 462 + 22x + 21x + x^{2}$$

$$x^{2} + 43x - 138 = 0$$

$$(x+46)(x-3) = 0$$

(rejected) x = -46 or x = 3

14 A number of regular n-sided polygons are placed together in a ring to form a regular N-sided polygon as shown in the diagram below.

Regular n-sided polygon

N-sided polygon

(a) Show that  $N = \frac{2n}{n-4}$ .

Answor

$$\frac{180(n-2)}{n} \times 2 + \frac{180(N-2)}{N} = 360$$

$$2N(n-2) + n(N-2) = 2nN$$

$$2nN - 4N + nN - 2n = 2nN$$

$$2n = nN - 4N$$

$$N(n-4) = 2n$$

$$N = \frac{2n}{n-4}$$

(b) Hence, explain why a regular octagon cannot be formed by placing smaller n-sided regular polygons in a ring.

 $\Xi$ 

Answer

$$\frac{2n}{n-4} = 8$$

$$n-4$$

$$2n=8n-32$$

$$6n = 32$$

$$n = \frac{16}{3}$$

It is not a octagon as n is not an integer.

2

Turn over

\_\_\_\_

10

15 (a) Express  $x^2 + 5x + 7$  in the form  $(x+a)^2 + b$ .

$$x^{2} + 5x + 7 = \left(x + \frac{5}{2}\right)^{2} - \left(\frac{5}{2}\right)^{2} + 7$$
$$= \left(x + \frac{5}{2}\right)^{2} + \frac{3}{2}$$

Answer ......[2]

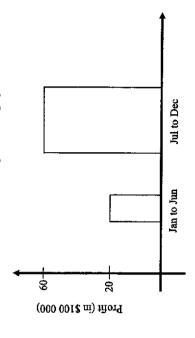
(b) Hence, explain why the expression will never be negative.

zswer.

Since 
$$\left(x+\frac{5}{2}\right)^2 \ge 0$$
 for all  $x$ ,  $\left(x+\frac{5}{2}\right)^2 + \frac{3}{4} \ge \frac{3}{4}$ . Therefore the expression will never be negative.

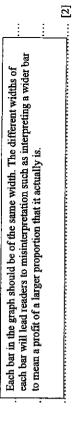
[1]

16 A company presented their 2023 financial report in this graph.



State one aspect of the graph that may be misleading and explain how they may lead to a misinterpretation.

Answer



**=** 

 $\varepsilon = \{ \text{integer } x \colon \ 0 < x \le 12 \}$ 

17

 $A = \{ \text{prime numbers} \}$ 

 $B = \{$  numbers that have at least 2 distinct factors $\}$ 

(a) Explain why A is a proper subset of B without listing down the elements.

Answer Prime numbers have 2 distinct factors, therefore every element of set A must also be an element of set B. However, some elements in B are composites and therefore not in Set A. Thus A is a proper subset of B.

(b) Draw a Venn diagram and list down the elements to illustrate the above information.

2

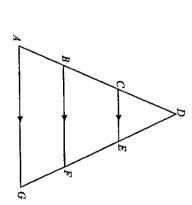
Answer

çn 12 10

 $\overline{2}$ 

18 The diagram shows a triangle AGD with the points C and B lying on AD and points E and F lying

12



It is given that CE/BF/AG, BF = 2CE and AG = 3CE

(a) Show that triangle DCE is similar to triangle DBF

Answer

 $\angle CDE = \angle BDE$  (common angle)  $\angle DCE = \angle DBF$  (corresponding angles)

.. Triangle DCE is similar to triangle DBF

(b) Given that the area of trapezium  $BFEC = 15 \text{ cm}^2$ , find the area of trapezium AGFB.

2

Area of 
$$\triangle DCE$$
Area of  $\triangle DBF$ 

$$\frac{A}{A} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}^{2} = \frac{1}{4}$$
Area of  $\triangle DAE$ 
Area of  $\triangle DAG$ 

$$\frac{1}{3} = \begin{pmatrix} 1 \\ 3 \end{pmatrix}^{2} = \frac{1}{9}$$
area of trapezium  $AGFB$ 
area of trapezium  $AGFB$ 

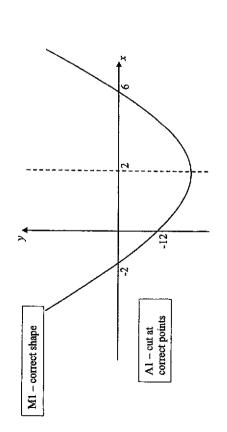
$$\frac{9-4}{4-1} = \frac{5}{3}$$

area of trapezium AGFB area of trapezium BFEC

area of trapezium  $AGFB = 25 \text{ cm}^2$ 

Answer ......cm<sup>2</sup> [3]

19 Sketch the graph of y = (2+x)(x-6) on the axes below. Indicate clearly the values where the graph crosses the axes and write down the equation of the line of symmetry.



x = 2Answer line of symmetry: ......

Find the percentage change in x when the value of y decreases by 50%. It is given that y is inversely proportional to the square root of x.

ನ

 $\sqrt{x} = \frac{k}{-}$  $y = \frac{k}{\sqrt{x}}$ 

 $\text{new } x = \frac{k^2}{\left(0.5y^2\right)}$ 

Percentage change in  $x = -\lambda^{-}$ 

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Turn over

2

Answer

14

21 The table shows the prices of movie tickets categorised by different days of the week and the various age groups.

	Monday to	Friday	Saturday and
	Thursday		Sunday
Child	00'9\$	\$8.50	\$9.00
Adult	00.78	\$10.00	\$12.50
Senior Citizen	05'98	00 6\$	\$10.00

(a) Write down a 3×3 matrix P to represent the above information.

family comprises three children and two adults. Represent this information as a The Ng family comprises a child, two adults and a senior citizen while the Tan 2×3 matrix Q. (E)

Answer P=....[1]

$$\mathbf{Q} = \begin{pmatrix} 1 & 2 & 1 \\ 3 & 2 & 0 \end{pmatrix}$$

Answer Q =....[1]

(ii) Evaluate QP and explain what the elements represent.

$$\mathbf{QP} = \begin{pmatrix} 1 & 2 & 1 \\ 3 & 2 & 0 \end{pmatrix} \begin{pmatrix} 6 & 8.5 & 9 \\ 7 & 10 & 12.5 \\ 6.5 & 9 & 10 \end{pmatrix}$$

 $= \begin{pmatrix} 26.5 & 37.5 & 44 \\ 32 & 45.5 & 52 \end{pmatrix}$ 

2 The elements in QP represent the respective total cost of movie tickets for the Ng family of I child, 2 adults and 1 senior citizen and the Tan Family of 3 children and 2 adults on the different days of the week.

Total time taken = 1 hour

Total distance travelled = 42 km

Let x be the distance between the breakfast place to office.

Distance between home to breakfast place = 42-x

Distance between home to break
$$V_1 = \frac{42 - x}{\left(\frac{15}{60}\right)} = 4\left(42 - x\right)$$

$$V_2 = \frac{x}{\left(\frac{1}{2}\right)} = 2x$$

$$V_3 = \frac{x}{\left(\frac{1}{2}\right)} = 2x$$

$$4\left(42 - x\right) - 2x = 10$$

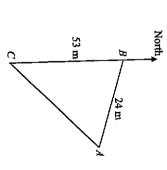
$$168 - 4x - 2x = 10$$

$$6x = 158$$
$$x = 26\frac{1}{3}$$

Answer ..... ....km [4]

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23 Three points A, B and C lie on a horizontal ground are such that AB = 24 m and BC = 53 m. Point B is due north of C. The bearing of A from B is  $122^{\circ}$ .



(a) Find the distance AC

$$AC = \sqrt{53^2 + 24^2 - 2(53)(24)\cos 58}$$
  
= 45.13186...  
= 45.1 (3sf)

(b) Find the bearing of C from A.

 $\frac{\sin \angle BAC}{53} = \frac{\sin \angle ABC}{45.13186...}$  $\sin \angle BAC = 53 \times \frac{\sin 58^{\circ}}{45.13186...}$ By sine rule,

Bearing of C from  $A = 360^{\circ} - 58^{\circ} - 84.8060...^{\circ}$  $=217.2^{\circ}$ 

 $\angle BAC = 84.8060...$ 

Answer ...... [3]

(c) Find the area of the triangular plot ABC. Area of  $\triangle ABC = \frac{1}{2}(53)(24)\sin 58^{\circ}$ 

= 539.35...

24 The first four terms in a sequence of numbers are

$$3+k,1+k,-1+k,-3+k,...$$

where k is a constant.

(a) Find an expression in terms of n and k, for the nth term in this sequence.

$$T_n = 3 + k + (n-1)(-2)$$
  
=  $3 + k - 2n + 2$   
=  $5 - 2n + k$ 

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(a) State two conditions on k such that 39 is a term of the sequence.

Answer

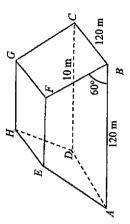
$$5 - 2n + k = 39$$

$$k-2n=34$$

$$k = 34 + 2n$$

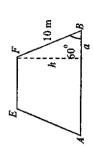
Since  $n \ge 1$ ,  $34 + 2n \ge 36$ , therefore  $k \ge 36$  and k must be an even number.

25 The diagram below shows an indoor adventure park in the shape of a trapezoidal prism with a square base ABCD. The indoor adventure park is positioned on horizontal ground and the walls ADEH and BCFG are slanted while the walls ABFE and DCGH are vertically upright.



The top of the prism, EFGH, is the ceiling of the adventure park which is also horizontal. EFGHis a square and the centre of *EFGH* lies vertically above the centre of *ABCD*. AB = 120 m, AE = BF = CG = DH = 10 m and  $\angle ABF = 60^{\circ}$ .

(a) Find the area of ABFE.



Since AE = BF, ABFE is an isosceles trapezium.

$$\sin 60^{\circ} = \frac{h}{10}$$

$$h = 10 \sin 60^{\circ}$$

[7]

$$\cos 60^\circ = \frac{a}{10}$$

$$a = 10\cos 60^{\circ}$$

Thus 
$$ER = 12 - 5 - 5 = 2$$
  
Area of trapezium  $ABFE = \frac{1}{2}(120 + 1)$ 

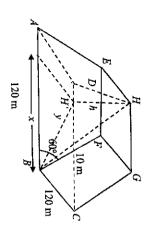
Area of trapezium 
$$ABFE = \frac{1}{2}(120 + 110)(8.660254...)$$

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[Turn over

3 The owner of the indoor park wants to build a flying fox feature from point H to point B. The angle of depression from point H to point B must not exceed  $S^\circ$ , in order to meet the safety requirements. Explain with mathematical workings whether the flying fox feature can be built.

Answer



$$x = 120 - 5$$
$$= 115$$

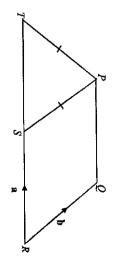
$$y = \sqrt{120^2 + 115^2}$$
$$= \sqrt{27625}$$

$$\tan \angle HBH' = \frac{8.660254...}{\sqrt{27625}}$$

By alternate angle, the angle of depression is  $3.0^\circ$  which is less than  $5^\circ$ , therefore the flying fox feature can be built.

[23]

26 In the diagram below, PQRST is a trapezium made up of a parallelogram PQRS and an isosceles triangle PST where PT = PS. It is given that  $\overline{RS} = a$ ,  $\overline{RQ} = b$  and SR = ST.



(a) Show that  $\overline{QS} = \overline{PT}$ .

Answer

$$\overline{QS} = \overline{QR} + \overline{RS}$$

$$\frac{=-\mathbf{b}+\mathbf{a}}{PT} = \overline{PS} + \overline{ST}$$

=-b+a

Therefore 
$$\overrightarrow{QS} = \overrightarrow{PT}$$
.

(b) Hence or otherwise, prove that the trapezium is made up of three isosceles triangles PST.

2

Since PQRS is a parallelogram, PS//QR, PQ//SR

PS = QR and PQ = SR

From (a), since  $\overline{QS} = \overline{PT}$ , thus PT = QS

PT = QS = PS = QR and PQ = SR = TS

By SSS congruency test, triangle PTS, triangle PQS and triangle QSR are congruent, therefore the trapezium is made up of three isosceles triangles PST.

<u>.</u>

Alternative solutions

11 [14(a)	
<del></del>	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
	n-4

Class Register Number: Class: Name:

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CHUNG CHENG HIGH SCHOOL (MAIN)

PRELIMINARY EXAMINATION 2024 SECONDARY 4

MATHEMATICS

Paper 2

Tuesday 20 August 2024

4052/02

2 hours 15 minutes

**MARKS SCHEME** 

Candidates answer on the Question Paper

Compound interest

Total amount =  $P\left(1 + \frac{r}{100}\right)^n$ 

Curved surface area of a cone =  $\pi r l$ 

Mensuration

Surface area of a sphere =  $4 \pi r^2$ 

Volume of a sphere  $= \frac{4}{3} \pi r^3$ Volume of a cone =  $\frac{1}{3}\pi r^2 h$ 

Area of triangle  $ABC = \frac{1}{2}ab\sin C$ 

Arc length =  $r \theta$ , where  $\theta$  is in radian

Sector area  $= \frac{1}{2}r^2\theta$ , where  $\theta$  is in radian

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2b \cos A$$

Statistics

$$\mathsf{Mean} = \frac{\Sigma f x}{\Sigma f}$$

Standard deviation =  $\sqrt{\frac{\Sigma f \kappa^2}{\Sigma f}} - \left(\frac{\Sigma f \kappa}{\Sigma f}\right)^2$ 

2024 Preliminary Exam/CCHMS/Secondary 4/Mathematics/4052/02

This document consists of 23 printed pages and 1 blank page.

2024 Preliminary Exam/CCHMS/Secondary 4/Mathematics/4052/02

Mathematical Formulae

Year	2020	2021	2022
Total Electricity		3	
Consumption in Gigawatt	50 779	53 483	54 884
Hours (GWh)			

In 2021, the electricity consumed by households took up 15.5% of the total electricity consumption. Calculate the amount of electricity consumed by households in 2021, correct to two significant figures.

Electricity consumed by household =15.5%×53483

= 8289.865

= 8300 GWh (2 s.f.)

Answer ..... GWh [1]

(ii) Calculate the percentage increase in the total electricity consumption from 2020 to

TURN OVER FOR QUESTION 1

Percentage increase =  $\frac{54884 - 50779}{50779} \times 100\%$ = 8.08%

Answer ......% [2]

(iii) Express the 2020 electricity consumption in kilowatt hours (kWh), leaving your answer in standard form, correct to two significant figures.

$$50779 \times 10^9 + 10^3 = 5.0779 \times 10^{10}$$
  
=  $5.1 \times 10^6$  kWh (2 s.f.)

Answer  $x = \dots$  [3]

- (b) A microprocessor is in the shape of a cube where the sides are 5 mm in length.
- Find the maximum number of microprocessors that can be placed into a container with dimensions 10 cm by 2 cm by 8 cm. €

$$\frac{10}{0.5} = 20$$

$$\frac{2}{0.5} = 4$$

$$\frac{8}{0.5} = 16$$

$$\therefore 20 \times 4 \times 16$$

$$= 1280$$

A model of the microprocessor was made to a scale of 10:1. Given that the surface area of microprocessor is 150 mm², find the surface area of the model Answer ..... [2] microprocessor in square centimetres. **3** 

Model: Actual (Linear Scale) 10:1 (Area Scale) 100:1

The surface area of the model is 100 times of the actual object.

 $= \frac{15000}{100} \text{ cm}^2$  $=15000 \, \mathrm{mm}^2$ Surface Area of Model =  $100 \times 150$  $=150 \, \text{cm}^2$ 

(a) Solve 2x-7=3(1-3x).

$$2x-7 = 3(1-3x)$$

$$2x-7 = 3-9x$$

$$11x = 10$$

$$x = \frac{10}{11}$$

(b) Solve the inequalities 7x-1<13 and  $\frac{x+1}{2}\ge -2(x-2)$ .

 $Answer x = \dots [2]$ 

 $1.14 \le x < 2$ 

(c) Rearrange the formula  $y = \frac{x^2 + 5}{7x^2}$  to make x the subject.

Answer ......[3]

$$y = \frac{x^{2} + 5}{7x^{2}}$$

$$7x^{2}y = x^{2} + 5$$

$$7x^{2}y - x^{2} = 5$$

$$x^{2}(7y - 1) = 5$$

$$x^{2} = \frac{5}{7y - 1}$$

$$x = \pm \sqrt{\frac{5}{7y - 1}}$$

Answer ..... cm² [2]

Turn over

cylinder has a base radius of 10 cm and a height of 20 cm. The frustum is formed by cutting a

smaller cone off the bottom of a larger cone. The smaller cone that was cut off has a height of The diagram shows two open containers, a right cylinder and an inverted frustum. The right

(d) Solve the equation  $\frac{2x}{1-x} - 3 = \frac{1}{2x-3}$ 

Give your solutions correct to two decimal places.

$$\frac{2x}{1-x} - 3 = \frac{1}{2x-3}$$

$$2x(2x-3) - 3(1-x)(2x-3) = 1-x$$

$$4x^2 - 6x - 3(2x-3-2x^2+3x) = 1-x$$

$$4x^3 - 6x - 6x + 9 + 6x^3 - 9x = 1-x$$

$$10x^2 - 20x + 8 = 0$$

$$5x^2 - 10x + 4 = 0$$

$$x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(5)(4)}}{2(5)}$$

$$x = 1.4472... \text{ or } 0.552786...$$

$$x = 1.45 \text{ or } 0.55 (2 \text{ s.f.})$$

x = 1.4472... or 0.552786...  $x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(5)(4)}}{}$ x = 1.45 or 0.55 (2 s.f.)

> and water is poured in to a depth of h cm. Three identical spherical marbles, each of radius 3 cm, are placed into the cylindrical container 4 cm. The larger cone has a base radius of 15 cm and a height of 12 cm. **10 cm**

(a) Find the volume of each marble, leaving your answer in terms of  $\pi$ .

Volume of each marble =  $\frac{4}{3}\pi(3)^3$ 

(b) Find the volume of the frustum, leaving your answer in terms of  $\pi$ .

Answer ...... cm<sup>3</sup> [1]

Volume of big cone =  $\frac{1}{3}\pi(15)^2(12)$ 

$$= 900\pi \text{ cm}^3$$

$$\frac{V_1}{V_2} = \left(\frac{l_1}{l_2}\right)^3$$

$$\frac{V_1}{900\pi} = \left(\frac{4}{12}\right)^3$$

$$V_1 = \frac{100}{3}\pi \text{ cm}^3$$

Volume of frustum =  $900\pi - \frac{25}{6}\pi$  $= \frac{2600}{3}\pi \text{ cm}^3$ 

Answer ...... cm<sup>3</sup> [3]

3

Find the value of h, correct to two decimal places.

Volume of water and marbles = 
$$\frac{2600}{3}\pi + 3(36\pi)$$

$$(10)^2 h \approx \frac{2924}{3} \pi$$

$$\pi(10)^{2} h = \frac{2924}{3} \pi$$

$$\frac{2924}{\pi(10)^{2}}$$

$$h = \frac{3}{\pi(10)^{2}}$$

$$h = 9.75$$

$$h = 9.75$$

<u>~</u>

The exterior surface area of each container is painted

ਉ

Find the total area painted.

$$l^2 = 12^2 + 15^2$$

$$l = \sqrt{369}$$
 cm

Surface area of cone =  $\pi(15)(\sqrt{369})$ 

$$\frac{A_1}{A_n} = \left(\frac{l_1}{L}\right)^2$$

=905.22036.. cm<sup>2</sup>

$$\frac{A_2}{A_2} = \left(\frac{1}{l_1}\right)$$

$$\frac{A_1}{m(15)(\sqrt{369})} = \left(\frac{4}{12}\right)^2$$

$$A_1 = 100.58004..$$
 cm<sup>2</sup>

$$\frac{15}{15} = \frac{12}{12}$$

$$15 \quad 12 \\ l_1 = 5 \text{ cm}$$

Surface Area of frustum = 
$$(905.22036..-100.58004..) + \pi(5)^2$$
  
=  $804.6403..+78.53981$ 

Answer ..... 2024 Preliminary Exam/CCHMS/Secondary 4/Mathematics/4052/02

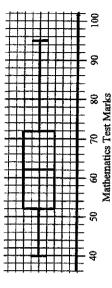
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12 students from class A took a Mathematics test. Œ

The table below shows the test marks of the students. However, two of the students' marks are covered with ink.

	<u> </u>	ľ	1
-	1	K	
	63	19	
	47	52	
	84	55	
	95	63	
	40	52	

Given that the box-and-whisker plot below shows the distribution of the results, explain why the information may not be sufficient to find the missing marks of he two students.  $\odot$ 



Answer

The box-and-whisker plot is not able to provide individual data point. It can only

provide the minimum, maximum mark, 25th, 50th and 75th perceptile and these data are insufficient to calculate the missing marks

(ii) Given further that the modal mark is 63, find the two missing marks.

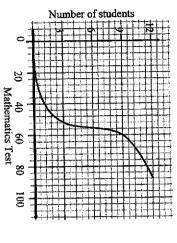
Since mode = 63, one of the missing marks = 63

Since upper quartile = 72,

$$\frac{63+x}{2} = 72$$

$$63 + x = 144$$
$$x = 81$$

Answer ...... and ..... [2]



Make a comment comparing the averages and a comment comparing the distribution of the Mathematics Test marks between the two classes.

The fouries to support your answers

distribution of the Mathematics 1est marks between the two chases.

Use figures to support your answers.

Generally, Class A did better. The median of Class A is 62 marks which is higher than the

median of Class B which is 56 marks. Interquartile range of Class A = 72 - 52 = 20

Interquartile range of Class B = 60 - 52 = 8

Since the interquartile range of Class A = 20 > the interquartile range of Class B = 8, the distribution of Class A's marks is more spread out than Class B's.

(3)
(b) Alice rolled a six-sided die, X, 100 times. Bala rolled another six-sided die, Y, 80 times
The number of times they each obtained a '6' is recorded in the table.

Y	X	Die
80	100	Number of rolls
18	16	Number of times '6' is obtained

Find the probability of rolling a '6' by Alice and Bala respectively.  $\frac{4}{25}$  or 0.16

Answer P(obtaining a '6' by Alice) =  $\frac{25}{9}$  or 0.225

P(obtaining a '6' by Bala) =  $\frac{40}{40}$  or 0.225

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(ii) One of the dice is biased. Using your answers in (b)(i), determine which die, X or Y, is likely to be the unbiased 6-sided die. Explain your answer.

Alice's die is more likely to be an unbiased die as the probability of getting a '6'

is closer to that of an unbiased die.

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5 (a) Complete the table of values for  $y = \frac{2}{x^2} - 2x$ 

Values are given to one decimal place where appropriate.

٠	*	*	
6.2		: اما	
4.5		-2	
4			
9		-0.5	
13.3		-0.4	
7		0.5	
0	-	1	
-13 -13 -13 -13 -13 -13 -13 -13 -13 -13		. 2	,
-5.8	,	ů.	,

(b) On the grid opposite, draw the graph of  $y = \frac{2}{x^2} - 2x$  for  $-3 \le x \le 3$ .

I I

(i) On the same grid, draw the graph of y+x=6 for  $-3 \le x \le 3$ .

3

γ	х
9	-3
w	ω

(ii) Write down the x-coordinates of the points where the line intersects the curve.

-0.6 0.55 Answer  $x = \dots$  and ...... [2]

(iii) These values of x are solutions of the equation  $x^3 + Ax^2 + B = 0$ . Find the value of A and of B.

$$6 - x = \frac{2}{x^2} - 2x$$
Multiply  $x^2$  thro

Multiply  $x^2$  throughout

$$6x^{2} - x^{3} = 2 - 2x^{3}$$
$$6x^{2} - 2 = -x^{3}$$
$$x^{3} + 6x^{2} - 2 = 0$$

A=6,B=-2

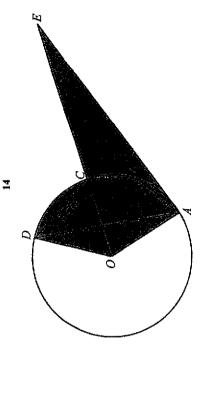
Answer A = .....





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AE is a tangent to the circle at A and OE is a straight line that passes through C. A, B, C and D are points on the circle with centre O and radius S cm. Angle  $OEA = 28^{\circ}$  and CD = 5 cm.

- (a) Find, giving a reason for each step of your working,
  - (i) angle OAD,

 $\angle OAE = 90^{\circ}$  (tangent perpendicular radius)

 $\angle COA = 180^{\circ} - 90^{\circ} - 28^{\circ}$  (angle sum of triangle)

 $\angle COD = 60^{\circ}$  (angle in an equilateral triangle)

 $\angle AOD = 60^{\circ} + 62^{\circ}$ 

=122°

 $\angle OAD = \frac{180^{\circ} - 122^{\circ}}{2}$  (base angles of an isosceles triangle)

Answer Angle OAD = ...... [3]

(ii) angle ABC.

reflex ∠COA = 360° - 62° (angles at a point)

 $\angle ABC = \frac{298^{\circ}}{2}$  (angle at center = twice angle at circumference) = 149°

Answer Angle ABC = ..... [2]

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(b) Find the area of the shaded region.

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Area of sector 
$$OCD = \frac{60^{\circ}}{360^{\circ}} (\pi)(5)^{2}$$

$$= \frac{25}{6} \pi = 13.089969... \text{cm}^{2}$$

$$= \frac{5}{4E}$$

$$AE = \frac{5}{4E}$$
Area of triangle =  $\frac{1}{2} \times \frac{5}{\tan 28^{\circ}} \times 5$ 

$$= \frac{25}{2 \tan 28^{\circ}} \times 5$$
Area of shaded region = 13.089969... + 23.50908...
$$= 36.6 \text{ cm}^{2} (3s.f)$$

 $=36.6 \text{ cm}^2 (3\text{s.f})$ 

Answer ..... .....cm<sup>2</sup> [4]

(a) A, B, C and D are four points such that the coordinates of A and C are (4,2) and

(10,-34) respectively. 
$$\overline{AB} = \begin{pmatrix} -9 \\ -12 \end{pmatrix}$$
 and  $\overline{AD} = \begin{pmatrix} 24 \\ -12 \end{pmatrix}$ .

(i) Find the coordinates of B.

$$\overline{AB} = \overline{OB} - \overline{OA}$$

$$\begin{pmatrix}
-9 \\
-12
\end{pmatrix} = \overline{OB} - \begin{pmatrix}
4 \\
2
\end{pmatrix}$$

$$\overline{OB} = \begin{pmatrix}
-5 \\
-10
\end{pmatrix}$$

$$B(-5, -10)$$
Answer (......) [1]

(ii) Find 
$$|\overline{AB}|$$
.
$$|\overline{AB}| = \sqrt{9^2 + 12^2}$$

$$= 15$$

It is given that E is a point on BD such that  $\overrightarrow{BE} = \frac{1}{3}\overrightarrow{BD}$ Answer  $|\overline{AB}| = \dots$  units [1]

(iii) Show that A, C and E are collinear.
Answer

$$\overline{BE} = \frac{1}{3} \begin{pmatrix} 33 \\ 0 \end{pmatrix} = \begin{pmatrix} 11 \\ 0 \end{pmatrix}$$

$$\overline{BE} = \overline{BA} + \overline{AE}$$

$$\begin{pmatrix} 11 \\ 0 \end{pmatrix} = \begin{pmatrix} 9 \\ 12 \end{pmatrix} + \overline{AE}$$

$$\overline{AE} = \begin{pmatrix} 2 \\ -12 \end{pmatrix}$$

$$\overline{AC} = \begin{pmatrix} 10 \\ -34 \end{pmatrix} - \begin{pmatrix} 4 \\ 2 \end{pmatrix}$$

$$= \begin{pmatrix} 6 \\ -36 \end{pmatrix}$$

$$\therefore \overline{AC} = 3\begin{pmatrix} 2 \\ -12 \end{pmatrix} = 3\overline{AE}$$

Since  $\overline{AE} = \frac{1}{3}\overline{AC}$  and with a common point A, therefore A, C and E are collinear.

- (b) A is the point (2,6), B is the point (-4,-2) and C is the point (6,-2). A line L passes through point C and is parallel to AB.
- (i) Find the equation of line L.

$$m_{AB} = \frac{6 - (-2)}{2 - (-4)}$$

$$= \frac{8}{6} = \frac{4}{3}$$
equation of line L:

$$y - (-2) = \frac{4}{3}(x - 6)$$

$$y+2 = \frac{4}{3}x - 8$$
$$y = \frac{4}{3}x - 10$$

$$y = \frac{4}{3}x - 10$$

Answer ..... [2]

Point D lies on line L such that AD // BC

- (ii) Find the coordinates of point D.
- AD = BC = 10 units

Since AB//CD and AD = AC, ABCD is a parallelogram.

thus 
$$AD //BC$$
.  
 $x_D = 2 + 10 = 12$ 

$$c_D = 2 + 10 = 12$$

$$y_p = \frac{4}{3}(12) - 10$$
  
= 6  
: D(12,6)

(iii) Show that ABCD is a rhombus

Answer D ( .....) [2]

$$AB = \sqrt{(2-(-4))^2 + (6-(-2))^2}$$

$$=\sqrt{100}=10 \text{ units}$$

$$\sqrt{100} = 10 \text{ units}$$

$$CD = \sqrt{(6 - (12))^2 + (-2 - 6)^2}$$
  
=  $\sqrt{100} = 10 \text{ units}$ 

= 
$$\sqrt{100}$$
 = 10 units  
 $BC = \sqrt{(6 - (-4))^2 + (-2 - (-2))^2}$ 

$$=\sqrt{100} = 10$$
 units

Since AD = BC = CD = AB = 10 units, : ABCD is a rhombus.

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2

(a) The figure shows the first three figures of a sequence formed by sticks of the same size.

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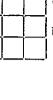


Figure 3 Figure 2 Figure 1

The number of small squares formed in each of the figures is recorded in the table.

Figure Number	Number of Squares
1	(1+1)²1
2	$(2+1)^2-1$
3	$(3+1)^2-1$

(i) Find the number of small squares formed in Figure 5. number of small squares formed in Figure 5 = 35 .....[1]

(ii) Find, in terms of n, an expression for the number of squares in Figure n.

expression for the number of squares =  $(n+1)^2 - 1$ 

Answer ......[1]

(iii) Explain why the sum of the number of squares in two consecutive figures is always

$$((n+1)^2-1)+((n+1+1)^2-1)$$

$$= n^{3} + 2n + 1 - 1 + n^{2} + 4n + 4 - 1$$
$$= 2n^{2} + 6n + 3$$

$$=2(n^2+3n)+3$$

Since  $2(n^2+3n)$  is a multiple of 2 which is an even number, and that 3 is an odd number therefore  $2(n^2 + 3n) + 3$  will always be odd.

(b) The table below shows the  $n^{th}$  terms of 4 sequences.

4	3	2	1	Sequence number
8n-1	14n	7n+1	4n+3	n <sup>th</sup> term

For each sequence, are the numbers in the sequence always multiples of 7, sometimes multiples of 7 or never multiples of 7?

Write down the letter 'A', 'S' or 'N' to represent your answer.

- Always multiples of 7
- Sometimes multiples of 7
- N Never multiples of 7

9 Sam is a 40-year-old man who earns a gross salary of \$8000 a month. He is a Singaporean and an employee of a Singapore firm. Sam is required to put a certain percentage of his monthly gross salary into his Central Provident Fund (CPF) account.

 ${\rm CPF}$  is a mandatory (social security) savings scheme funded by contributions from employers and employees. The table below shows the CPF contribution rates by employers and employees

Employee's age	CPF Contrib	CPF Contribution Rates from 1 January 2024 (Monthly gross salary > \$750)	muary 2024 750)
(Years)	Total (% of gross salary)	By Employer By Employee (% of gross salary) (% of gross salary)	By Employee (% of gross salar
55 and below	37	17	20
Above 55 to 60	31	15	16
Above 60 to 65	22	11.5	10.5
Above 65 to 70	16.5	9	7.5
Above 70	12.5	7.5	5

(a) Find the amount of money Sam's employer must contribute to his CPF monthly.

amount of money his employer must contribute =  $\frac{17}{100} \times $8000$ = \$1360

Answer \$.....[1]

Sam wants to plan his monthly savings and has tabulated his monthly expenditure as shown in the table. He hopes to save at least 20% of his salary each month after CPF deductions.

Expenditure	Amount (\$)
Food and Groceries	820
Transportation	90
Insurance and Healthcare	1000
Phone and Internet Subscriptions	80
Utilities	300
Housing Loan	1000
Leisure and Entertainment (movies snorts books subscription fees, dining etc)	1580

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Determine whether Sam is able to achieve his saving goals by clearly showing your calculations. **e** 

amount of money he must contribute to CPF = 
$$\frac{20}{100}$$
 ×\$8000

$$=$1600$$

total expenditure = 
$$820 + 90 + 1000 + 80 + 300 + 1000 + 1580$$

$$=$4870$$

Savings percentage = 
$$\frac{1530}{8000 - 1600} \times 100\%$$
  
= 23.90625..%

= 23.9% (3s.f.)

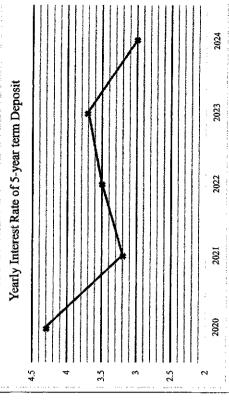
After a year of saving, Sam decides to invest \$15 000 of his savings for a period of 5 years. He comes up with 2 investment plans. 

_		
47 1164 Y	Sam can invest his money in a 5-year savings bond at the beginning of 2025. The interest	rate for the 5-year term is shown in the table. The savings bond compounds annually.

Year from issue date	-	2	3	4	5
Interest per year %	3.19	3.19	3.20	3.28	3.31

Sam can invest his money at the beginning of 2025 into an insurance company's fixed deposit account for a period of 5 years, compounded yearly. The interest rate is fixed over the duration of the investment and is determined by the year of issuance.

For example: If Sam had invested his money in 2020, over a period of 5 years, his investment plan would be at an interest of 4.3% compounded yearly over the period of 5 However, the interest rate for 2025 is not yet available. Sam finds the information about the interest rates offered by the insurance company for the last 5 years.



[Turn over

[4] ·····

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Justify the decision you make and show your calculations clearly.

Determine which plan Sam should choose.

Answer Plan A

	After 5th year		After 4th year		After 3 <sup>rd</sup> year		After first 2 years
= \$17587.52679 = \$17587.53 (nearest cent)	$A = (17024.03136)\left(1 + \frac{3.31}{100}\right)$	=\$17024.03136	$A = (16483.3766)\left(1 + \frac{3.28}{100}\right)$	= \$16483.3766	$A = (15972.26415)\left(1 + \frac{3.2}{100}\right)$	= \$15972.26415	$A = 15000 \left( 1 + \frac{3.19}{100} \right)^2$

Plan B

Average interest rate =  $\frac{4.3+3.2+3.5+3.7+3}{5}$ = 3.54

Amount after 5 years =  $15000\left(1+\frac{3.54}{100}\right)^5$ = \$17849.75 (nearest cents)

Since \$17849.75 > \$17587.53, Sam should consider Plan B.

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